

Physics-Informed Neural Networks for Heat Transfer Predictions in Additive Manufacturing

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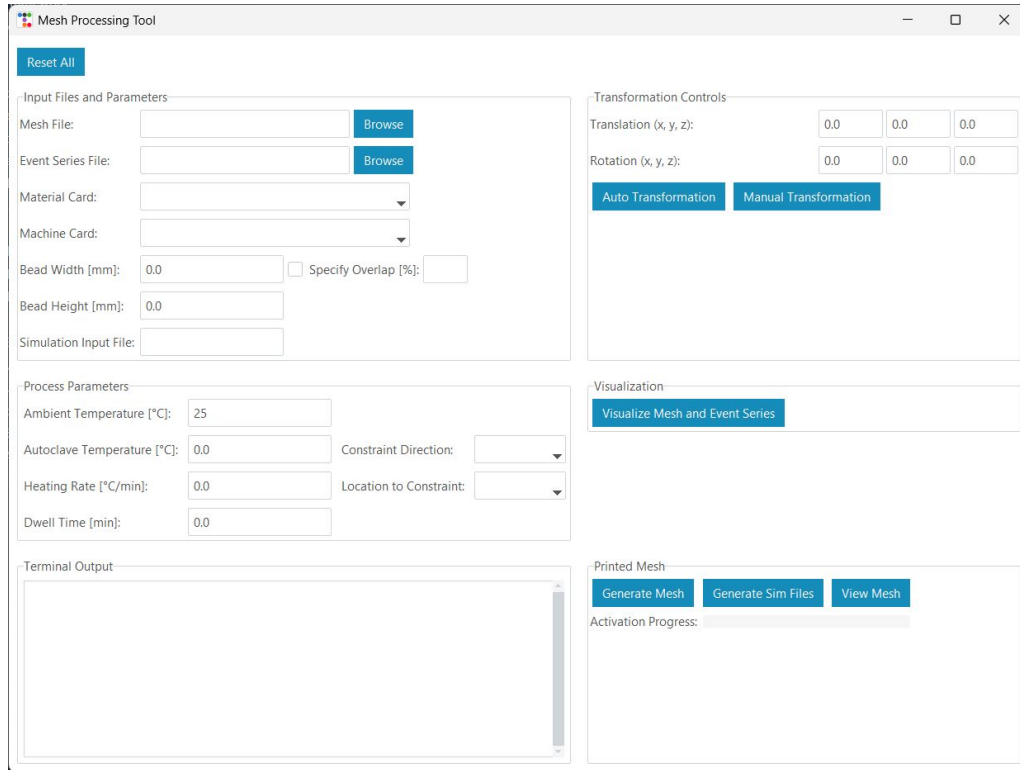
May 20, 2025

About

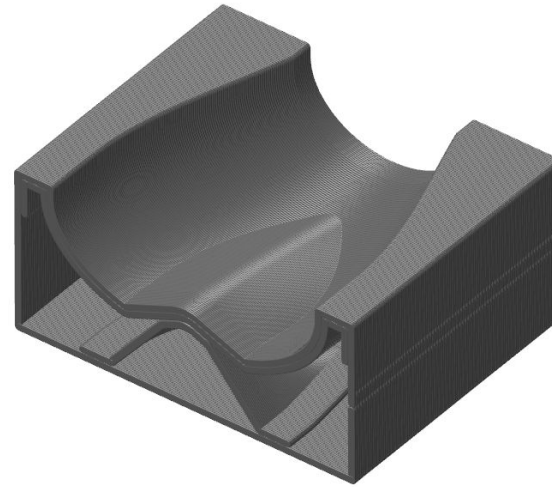
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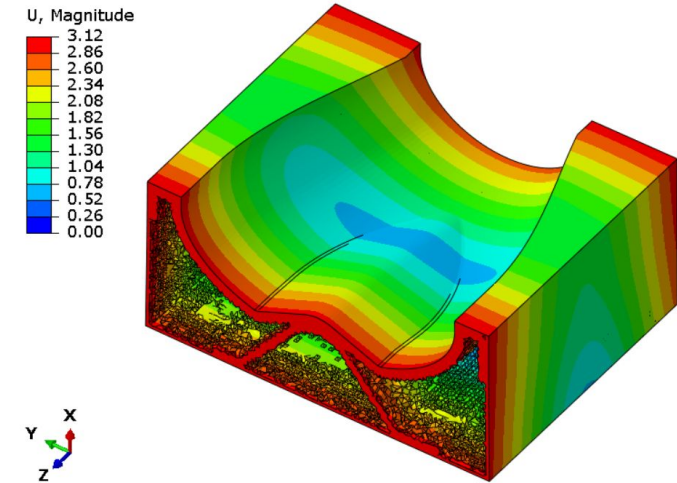
Other Research Projects



Graphical User Interface



LSAM Tool Design



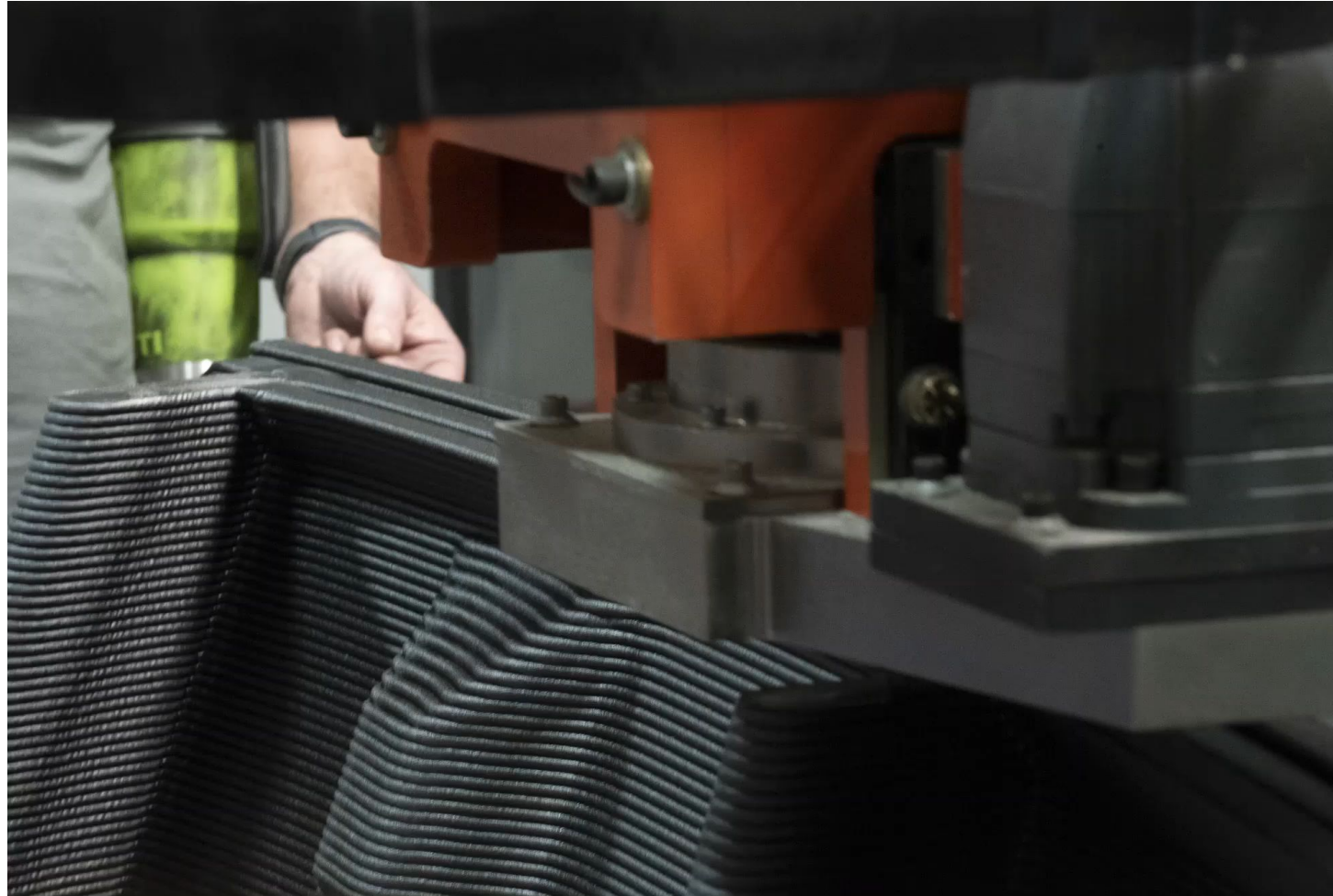
Shape
Compensation of
LSAM Tool Design

Thermwood LSAM Research Laboratory at Purdue

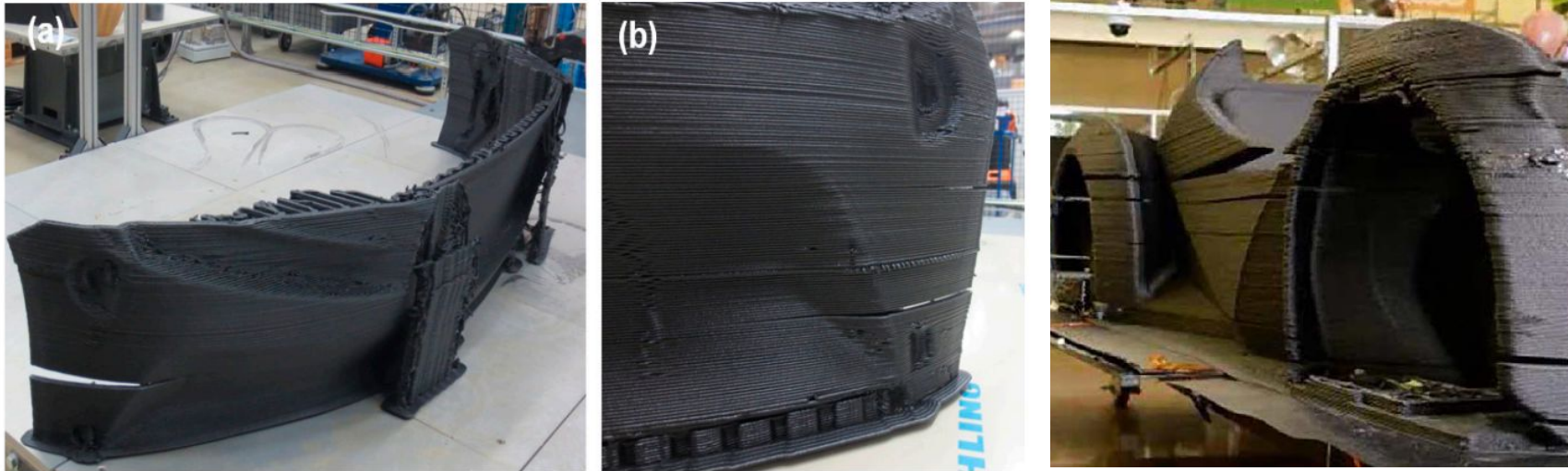
Goal: Support Thermwood and the Large-Scale Additive Manufacturing industry by delivering applied research and physics-based process simulations.



Large-Scale Additive Manufacturing



Potential Challenges



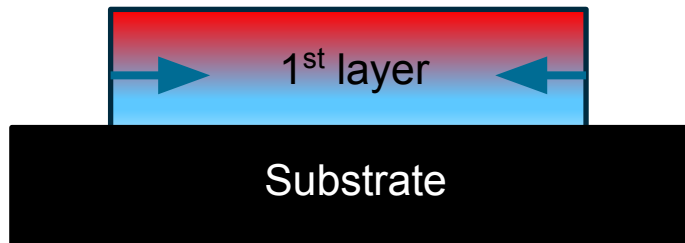
Akbari, S., Johansson, J., Johansson, E., Tönnäng, L., & Hosseini, S. (2022). Large-Scale Robot-Based Polymer and Composite Additive Manufacturing: Failure Modes and Thermal Simulation. *Polymers*, 14(9), 1731.

<https://doi.org/10.3390/polym14091731>

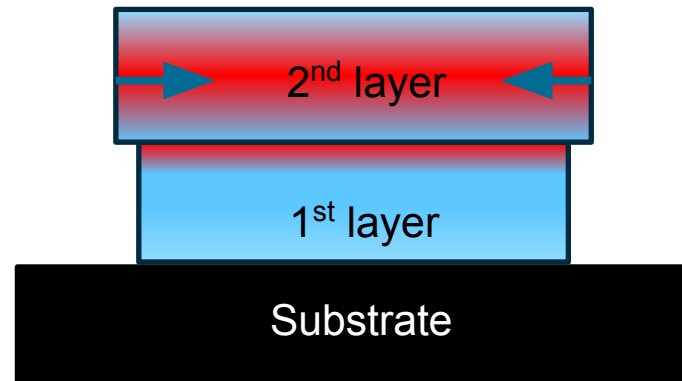
L. J. Love, "Utility of big area additive manufacturing (BAAM) for the rapid manufacture of customized electric vehicles," Oak Ridge National Laboratory (ORNL); Manufacturing Demonstration Facility (MDF), 2015.

Predicting Thermal History

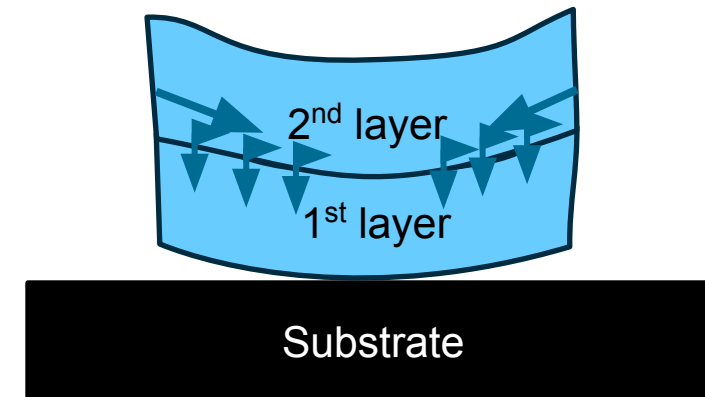
Thermal contraction



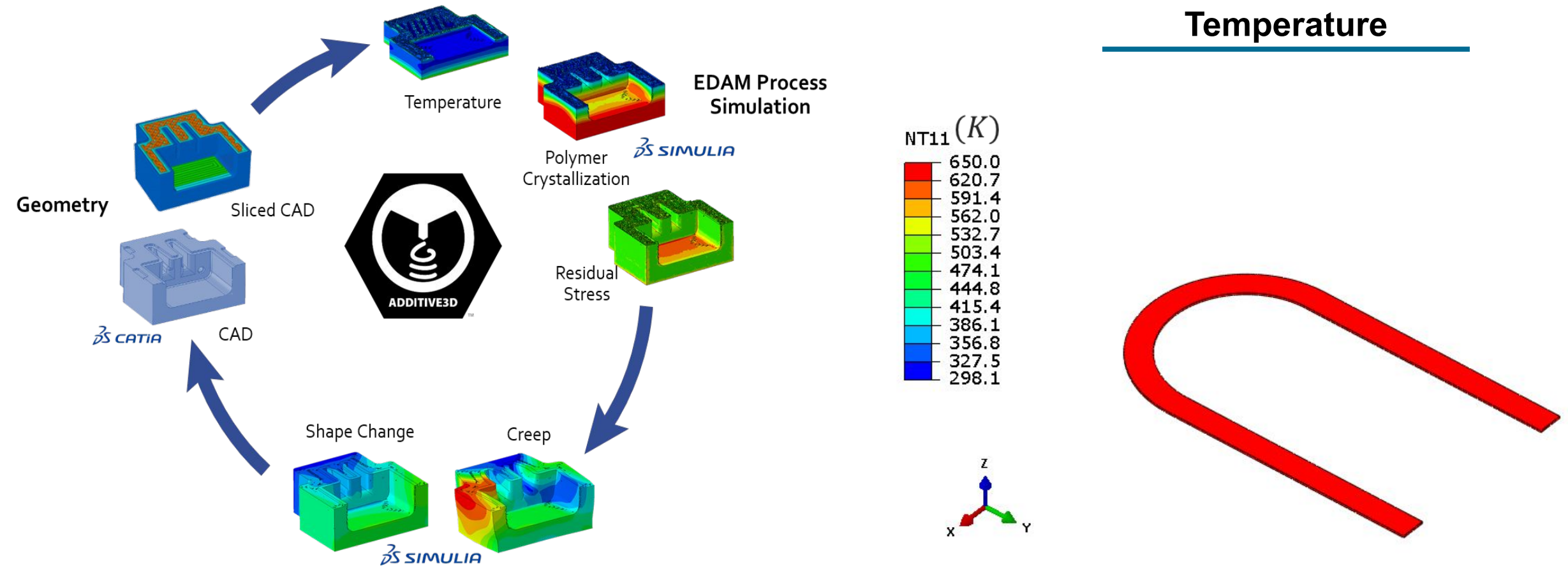
New hot layer placed on contracted cooled layer



Uneven cooling and contraction between layers causes warping



Finite Element Method (FEM)



Limitations of FEM

Requires discretization
in space and time



High computational costs

Limitations of FEM

Requires discretization
in space and time



High computational costs

Deterministic in nature
(1 input yields 1 output)



Inadequate for rapid exploration
of process parameters

Limitations of FEM

Requires discretization
in space and time



High computational costs

Deterministic in nature
(1 input yields 1 output)



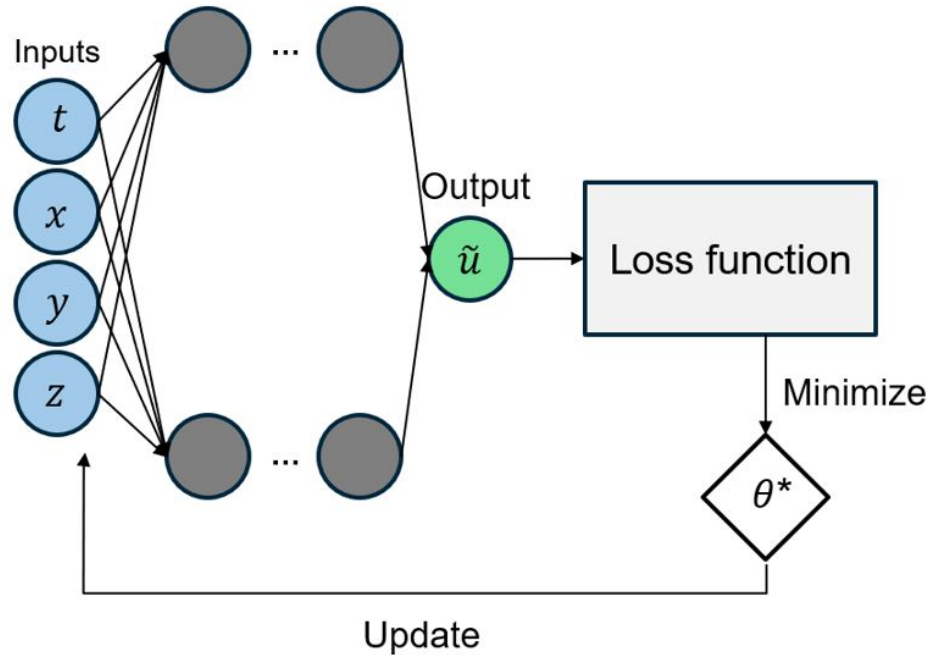
Inadequate for rapid exploration
of process parameters

Is there an alternative?

The Core of the Problem: Residual Minimization

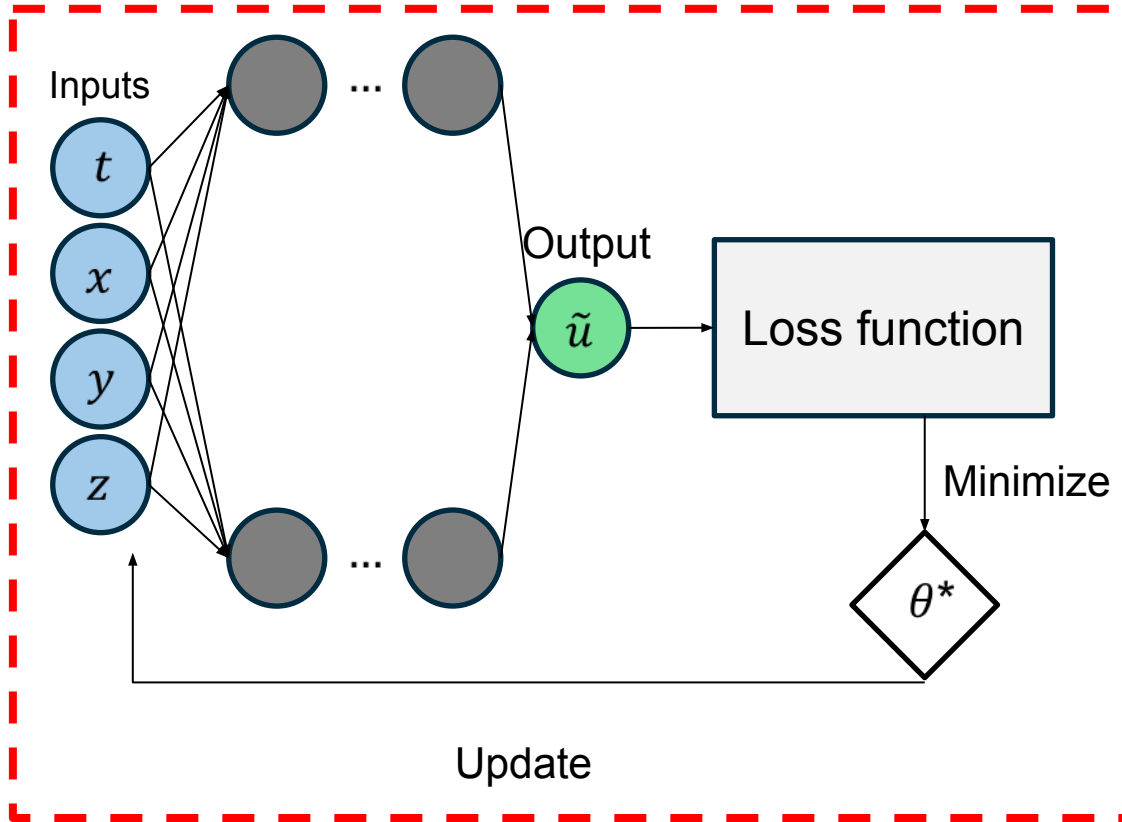
- Numerical methods solve PDEs by minimizing the residual
- Residual = PDE(Approximate solution) – Source Term
- To find an approximation solution $\hat{u}$ that minimizes this residual, a common strategy is to:
 - Define a loss function (e.g., MSE)
 - Choose a way to represent $\hat{u}$
 - Optimize the parameter of $\hat{u}$ to minimize the loss function

Neural Networks

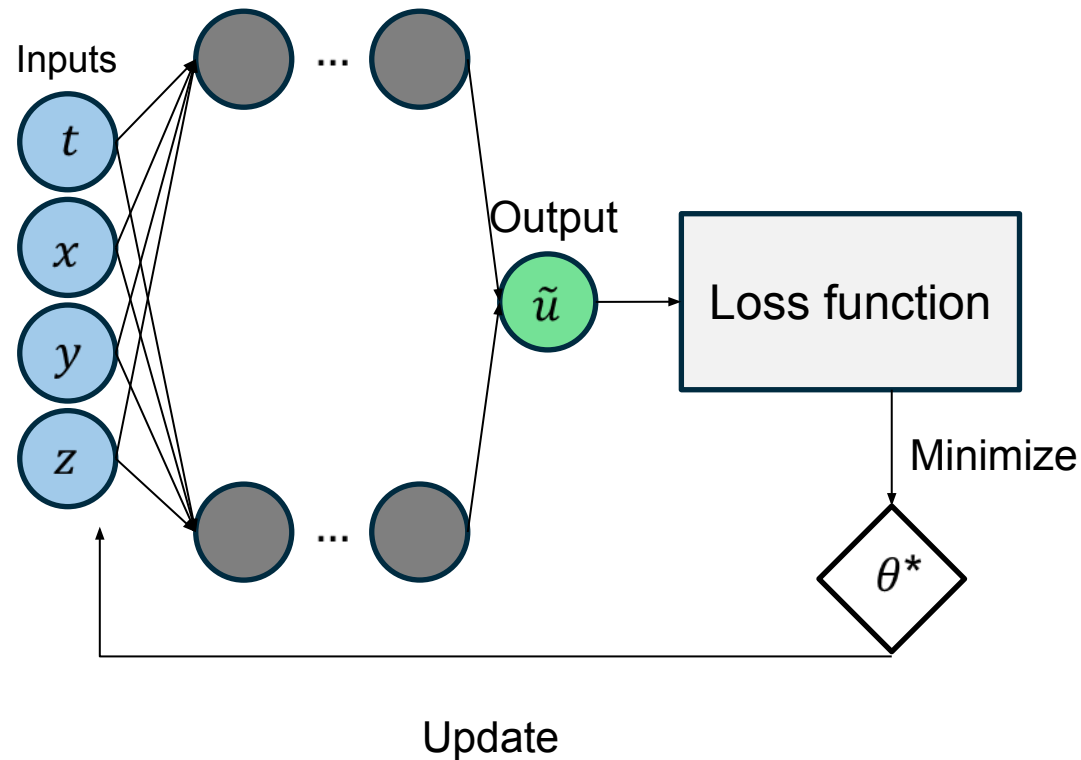


- Neural Network (NN) is denoted as $\hat{u}_\theta(X, t)$
- (X, t) are the input coordinates (space and time)
- θ is the network's learnable parameters
- θ is optimized by minimizing the loss function (predefined based on the PDE residual + boundary/initial conditions)
- The training process tunes θ so that $\hat{u}_\theta$ better satisfies the PDE

Physics-informed Neural Networks (PINNs)



Physics-informed Neural Networks (PINNs)



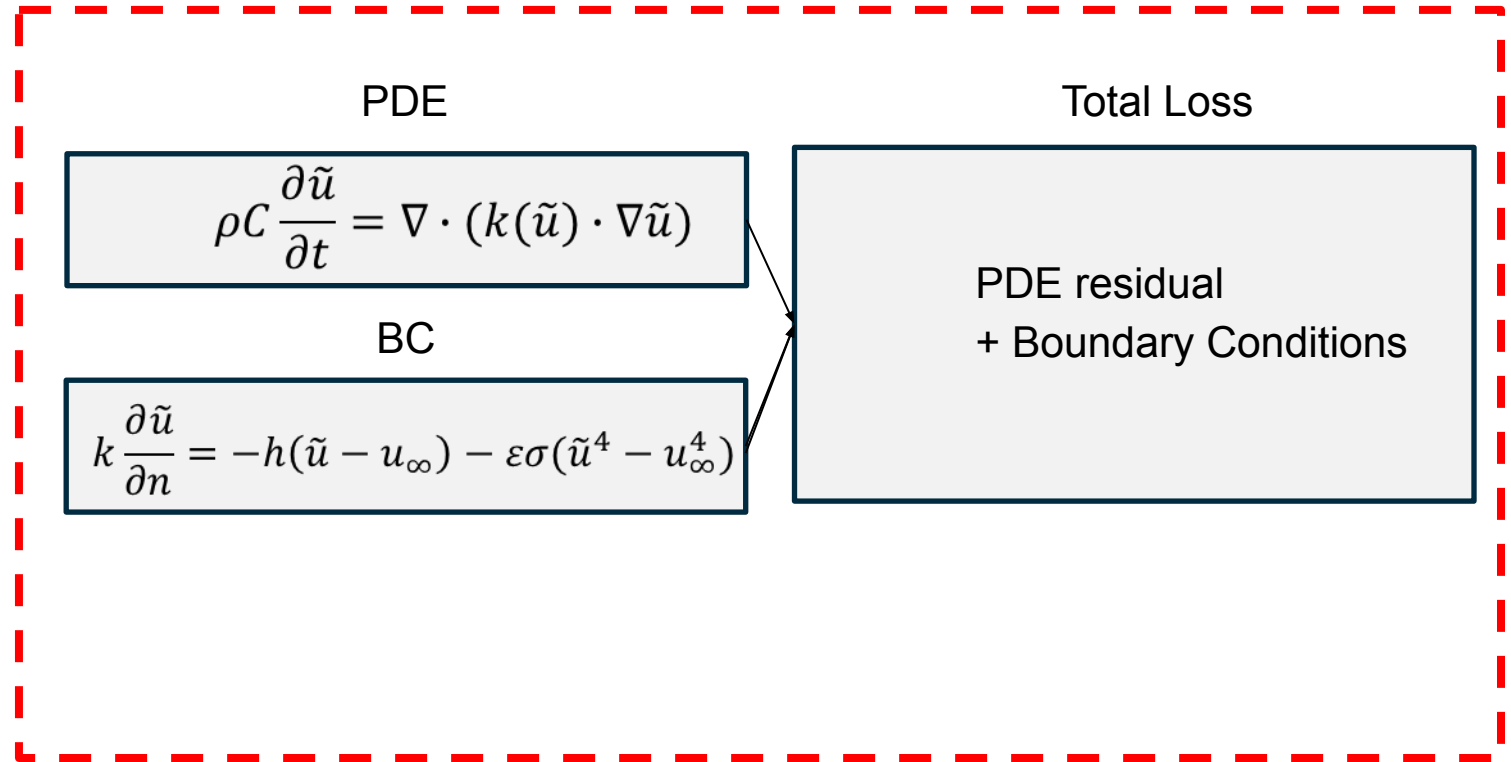
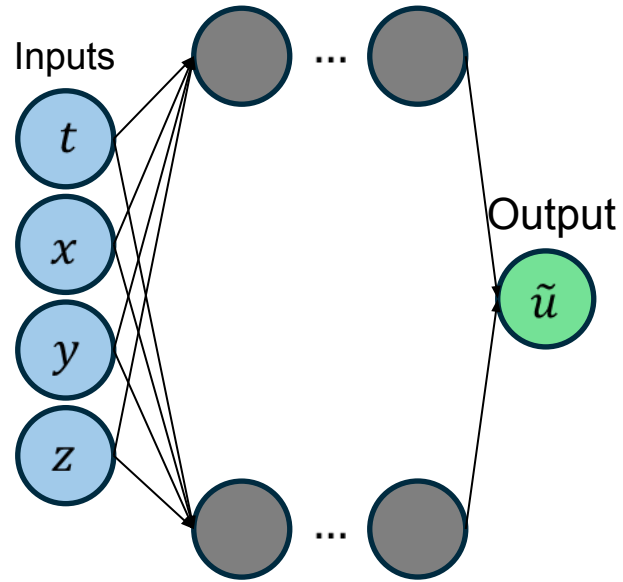
Governing Equation (PDE):

$$\rho C \frac{\partial u}{\partial t} = \nabla \cdot (k(u) \cdot \nabla u)$$

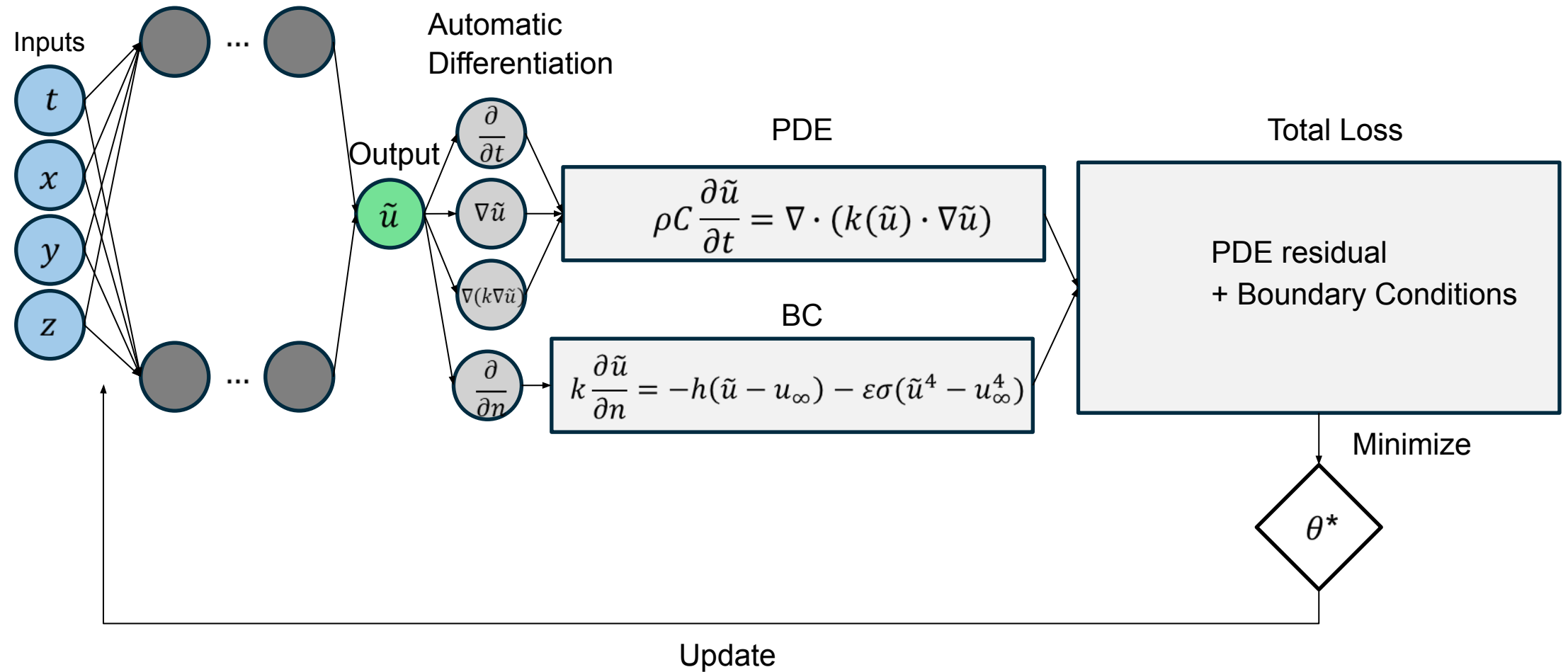
Boundary Condition (BC):

$$k \frac{\partial u}{\partial n} = \underbrace{-h(u - u_{\infty})}_{\text{Convection}} - \underbrace{\varepsilon \sigma (u^4 - u_{\infty}^4)}_{\text{Radiation}}$$

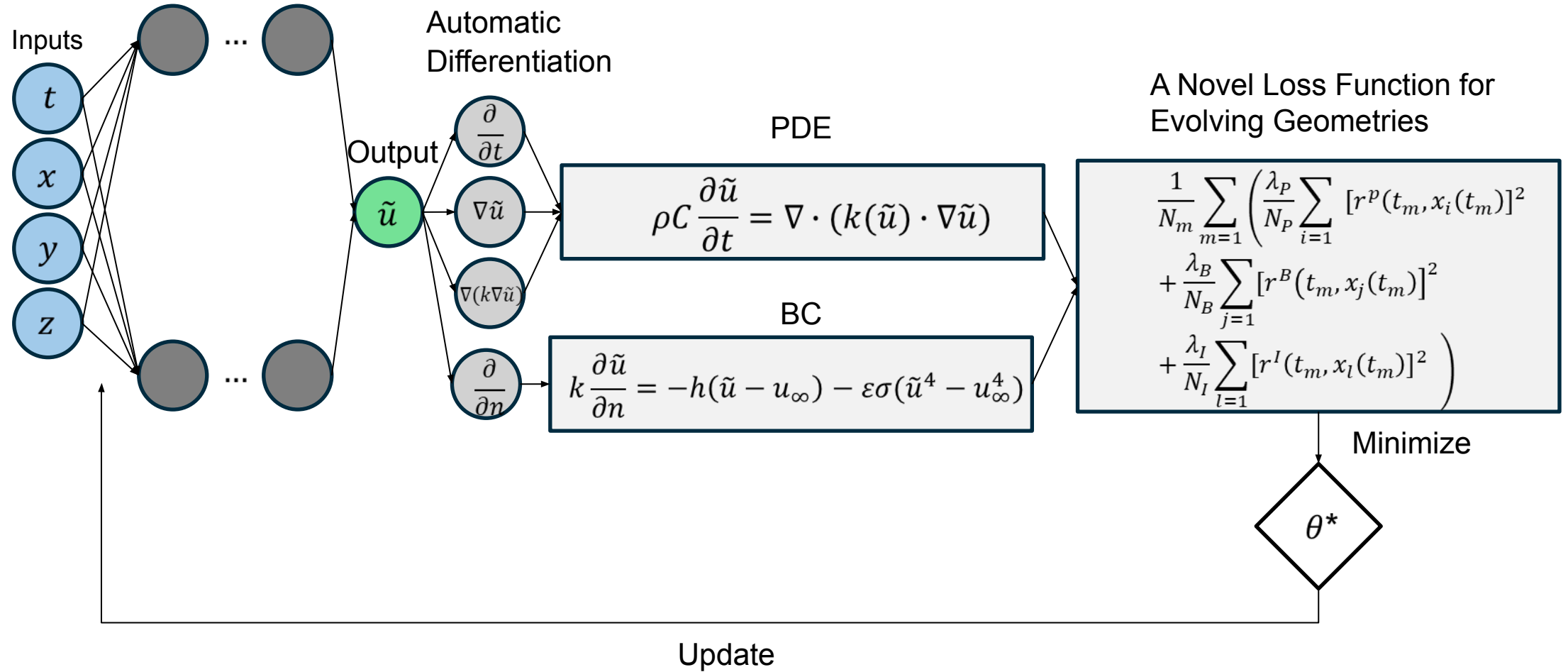
Physics-informed Neural Networks (PINNs)



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Physics-informed Neural Networks (PINNs)

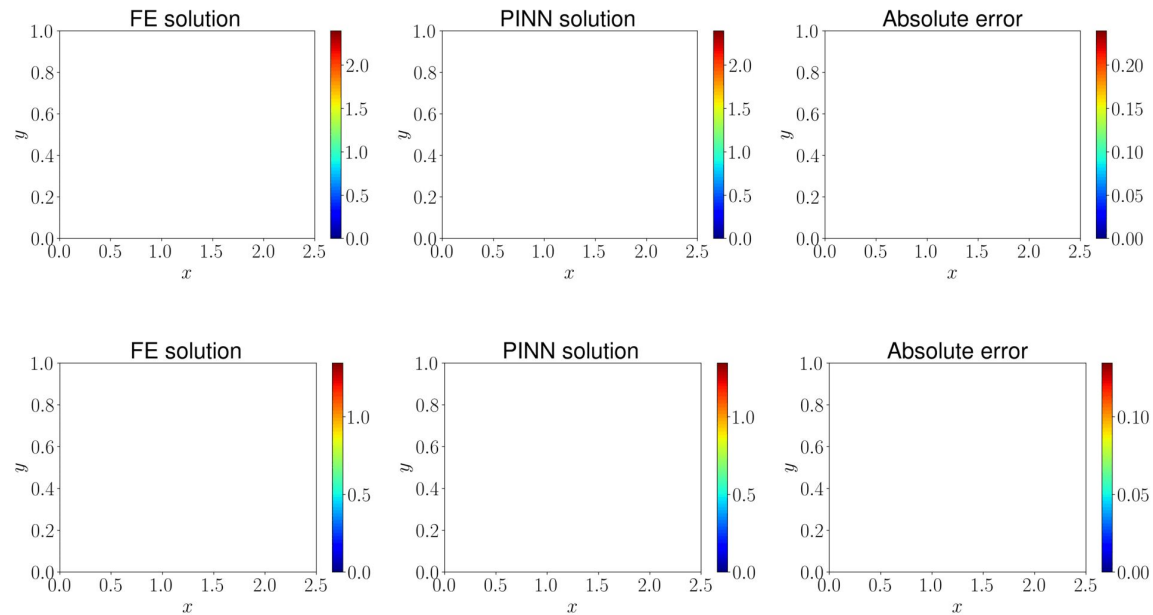


Aim of this work

Demonstrate the feasibility of using **PINNs** for **3D** transient heat transfer problem with **evolving** geometries and **complex boundary conditions**

Prior work

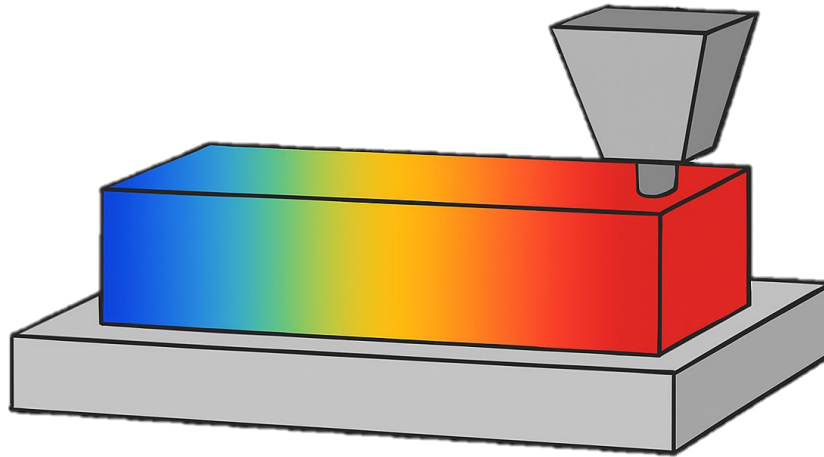
A. J. Thomas et al. (2025) “Causality enforcing parametric heat transfer solvers for evolving geometries in advanced manufacturing” *Computer Methods in Applied Mechanics and Engineering*



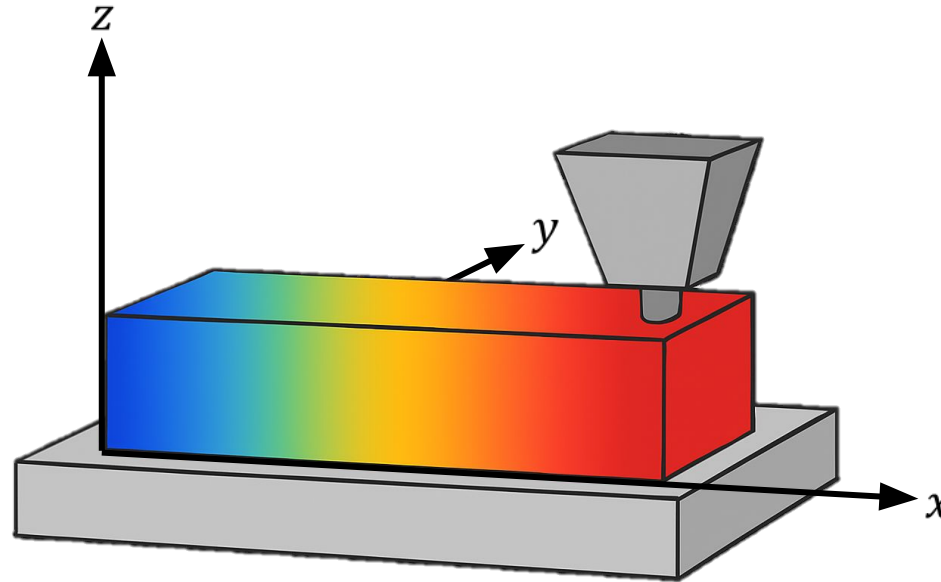
This work builds upon the above work. Specifically,

- **Extend** the formulation from **2D** to **3D** domain
- Incorporate physical complexities such as **radiation** and **temperature-dependent** properties

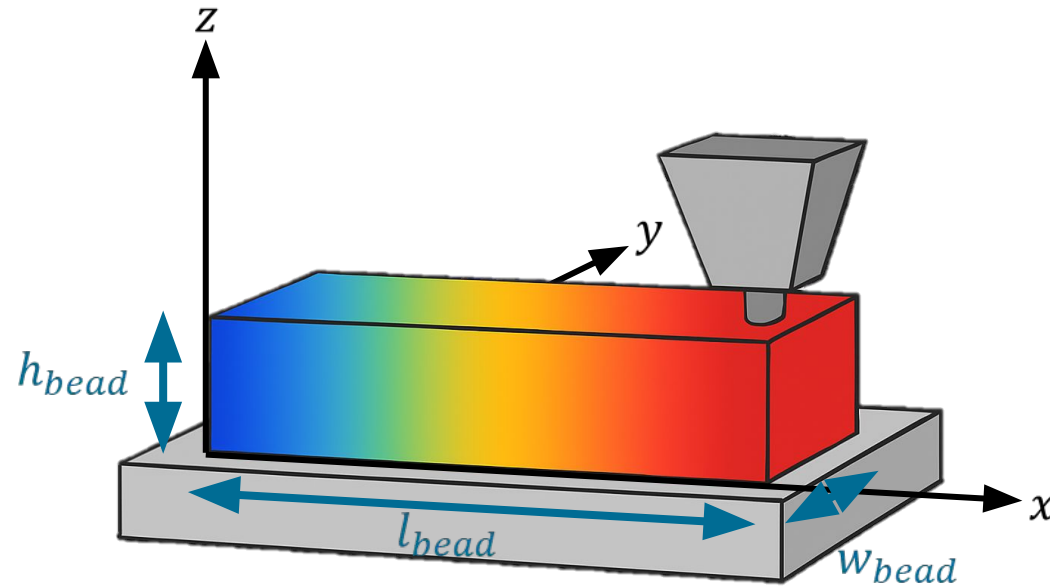
Methodology



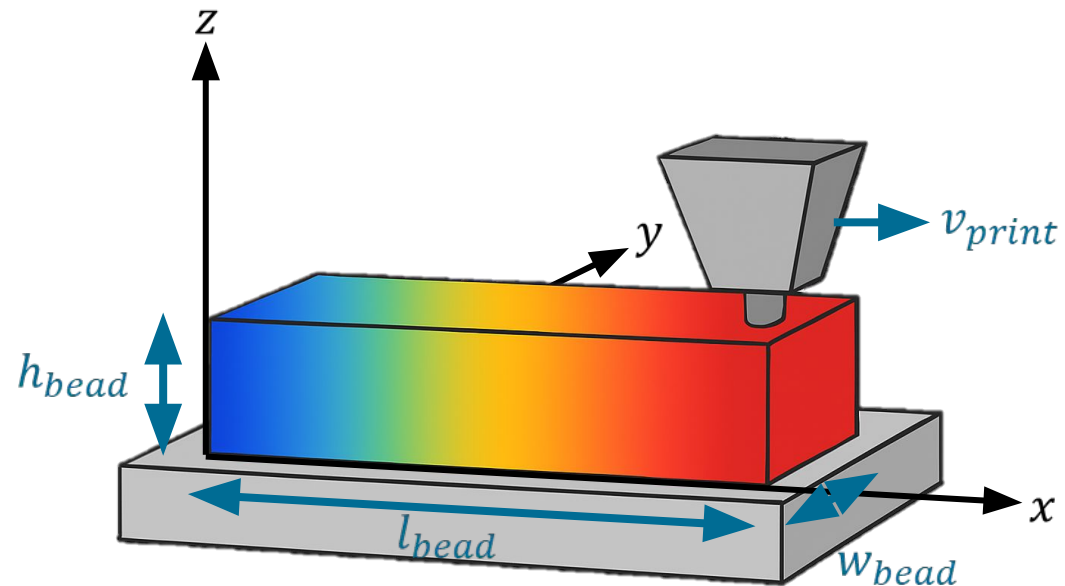
Domain Definition



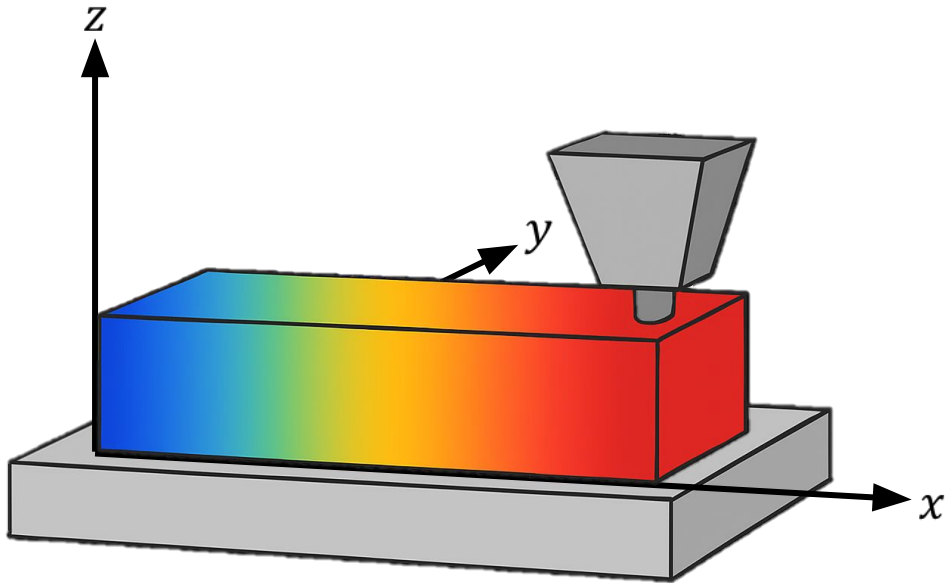
Domain Definition



Domain Definition



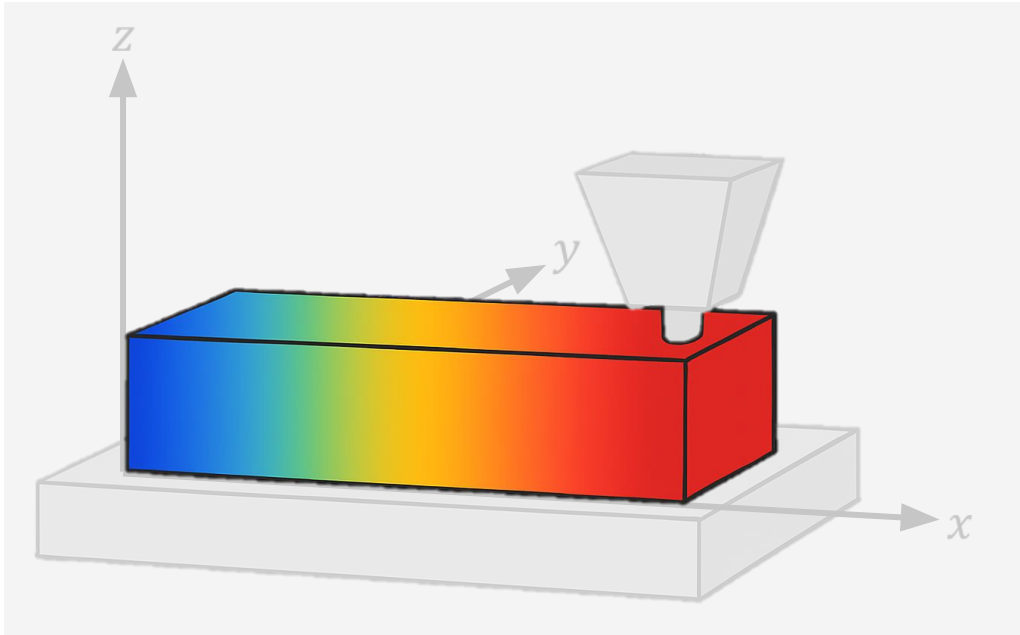
Physical Equations



Physical Equations

Governing Equation (PDE):

$$\rho C \frac{\partial u}{\partial t} = \nabla \cdot (k(u) \cdot \nabla u)$$

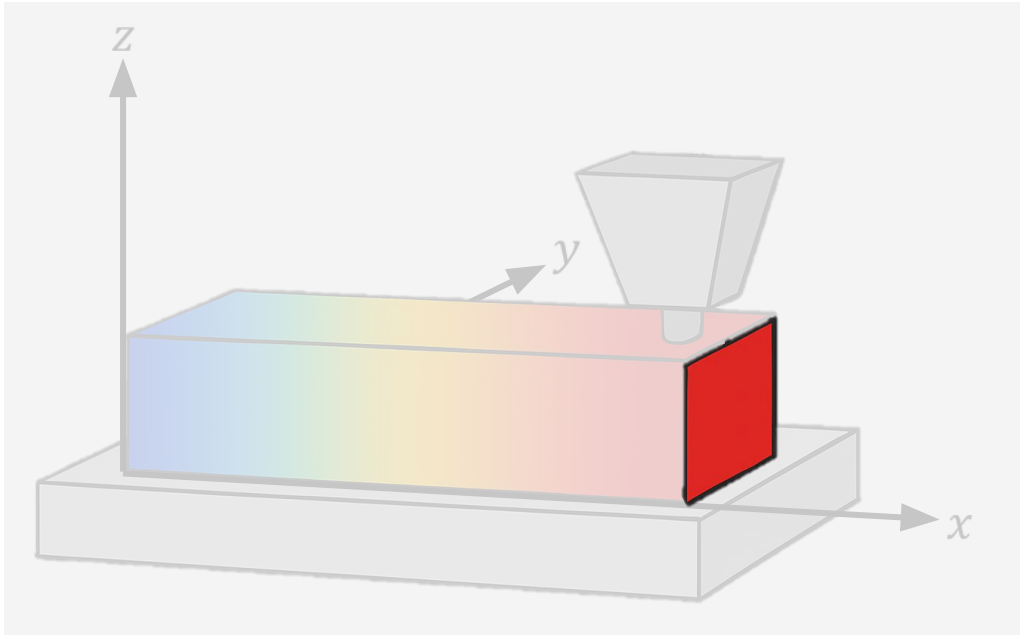


Physical Equations

Boundary Conditions (BC):

At deposition front:

$$u(x, y, z, t) = u_{dep}$$



Physical Equations

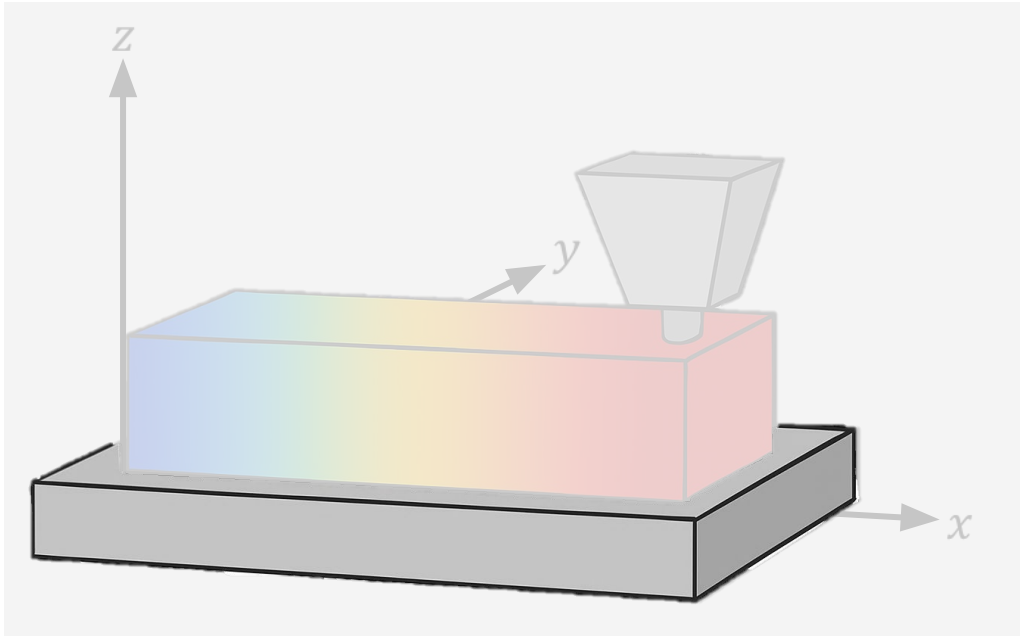
Boundary Conditions (BC):

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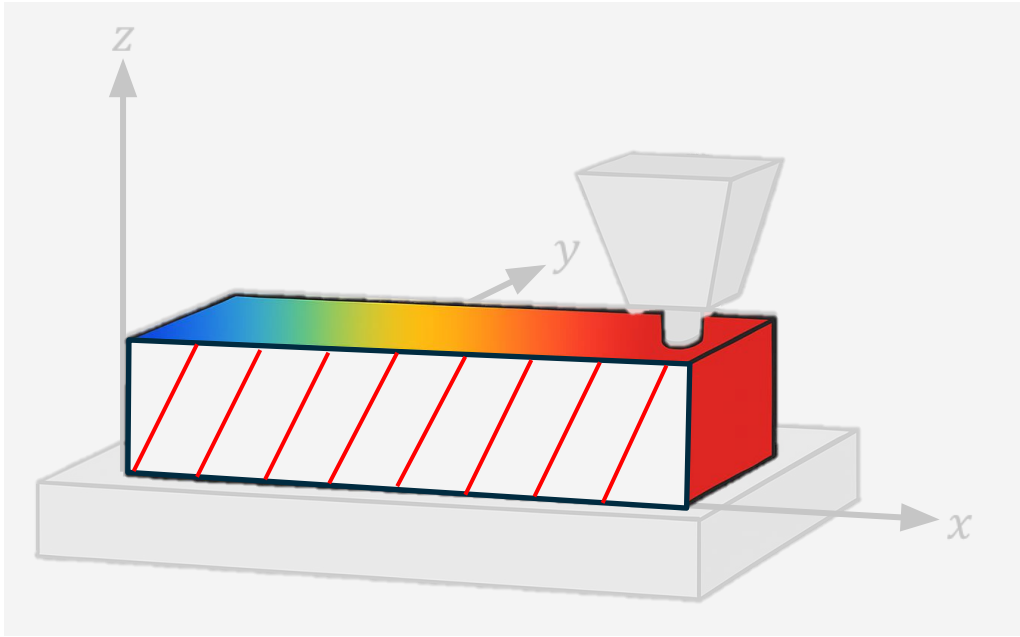
$$u(x, y, z, t) = u_{dep}$$

At print bed:

$$u(x, y, z, t) = u_{bed}$$



Physical Equations



Boundary Conditions (BC):

At deposition front:

$$u(x, y, z, t) = u_{dep}$$

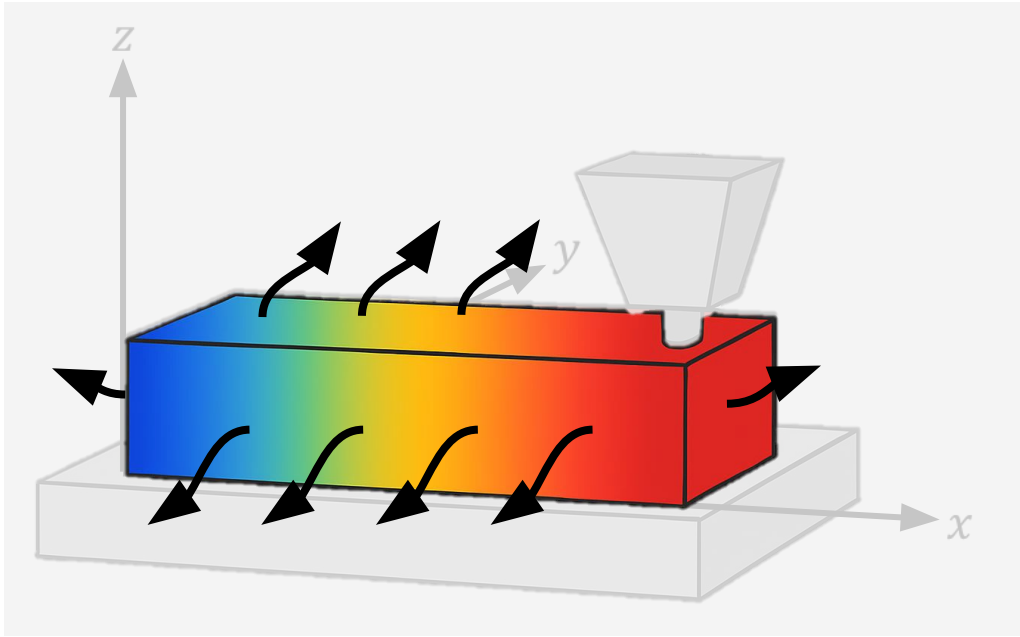
At print bed:

$$u(x, y, z, t) = u_{bed}$$

Adiabatic (no heat flux):

$$\frac{\partial u}{\partial n} = 0$$

Physical Equations



Boundary Conditions (BC):

At deposition front:

$$u(x, y, z, t) = u_{dep}$$

At print bed:

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Adiabatic (no heat flux):

$$\frac{\partial u}{\partial n} = 0$$

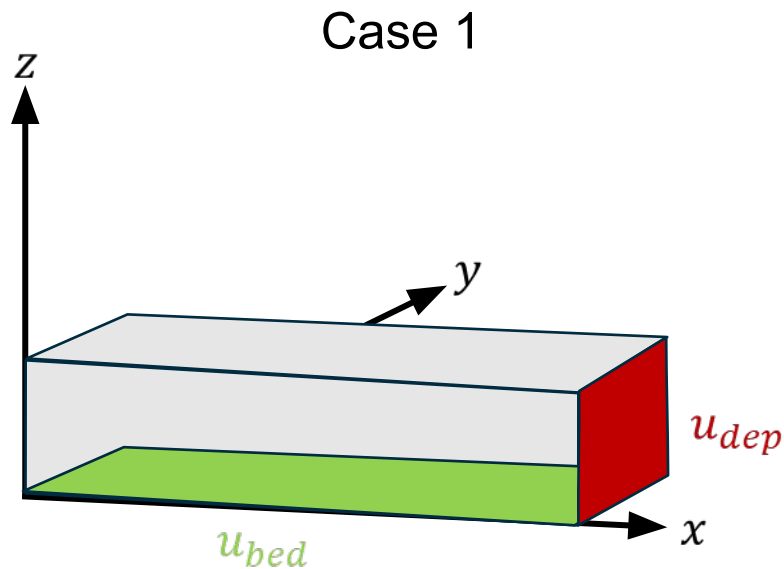
Convection:

$$k \frac{\partial u}{\partial n} = -h(u - u_{\infty})$$

Radiation:

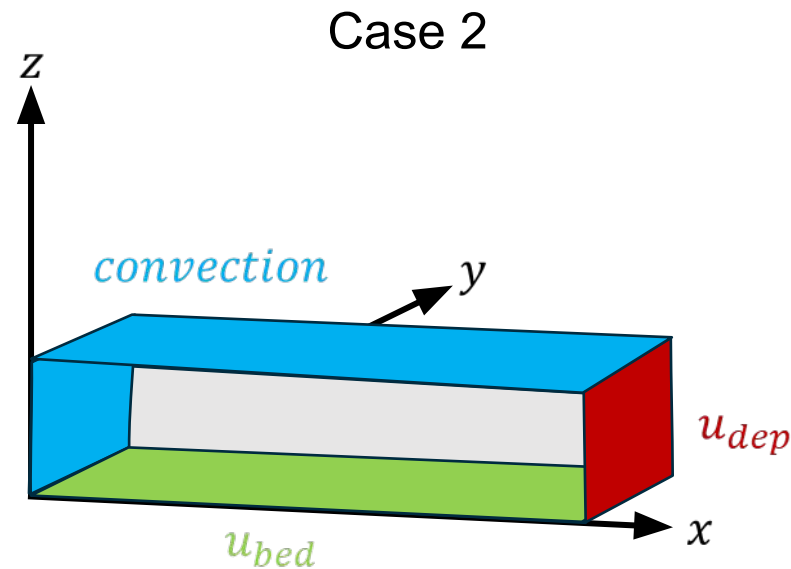
$$k \frac{\partial u}{\partial n} = -\varepsilon \sigma (u^4 - u_{\infty}^4)$$

Case Study: Evolving Geometries with Increasing Complexity



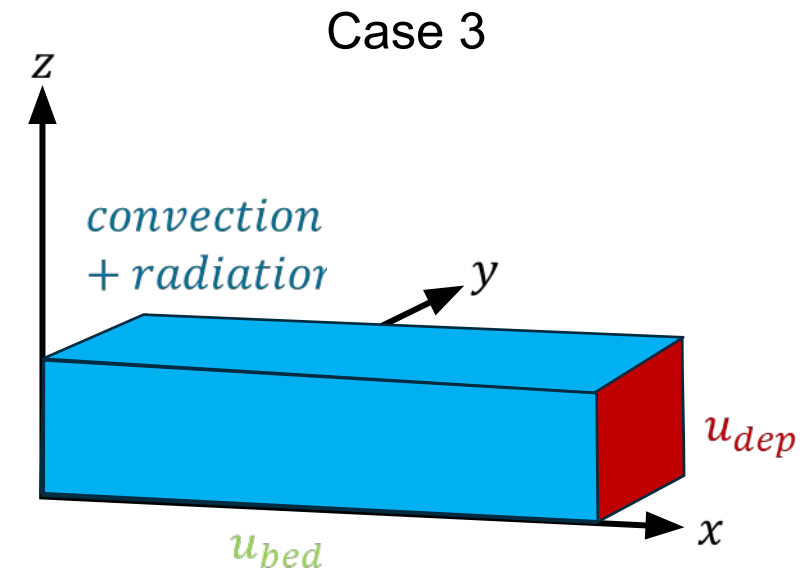
Conditions enforced:

1. Constant **deposition surface**
2. Evolving **bed surface**



Conditions enforced:

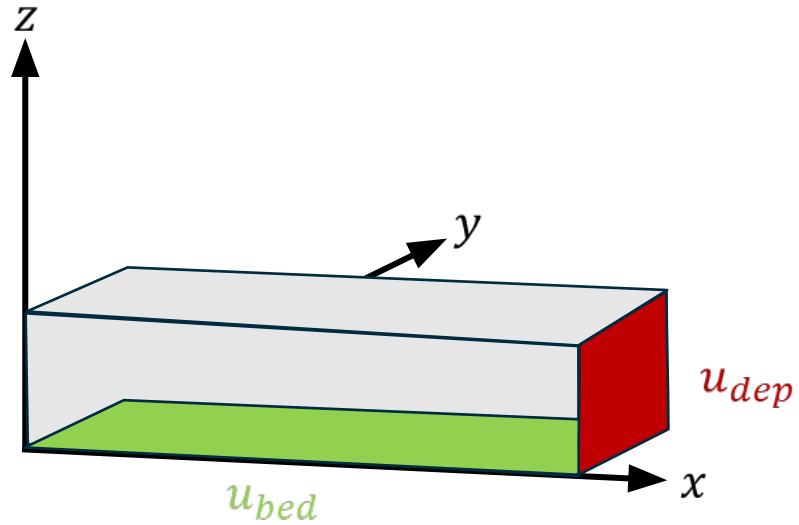
1. Constant **deposition surface**
2. Evolving **bed surface**
3. Constant and evolving surfaces with *convection*



Conditions enforced:

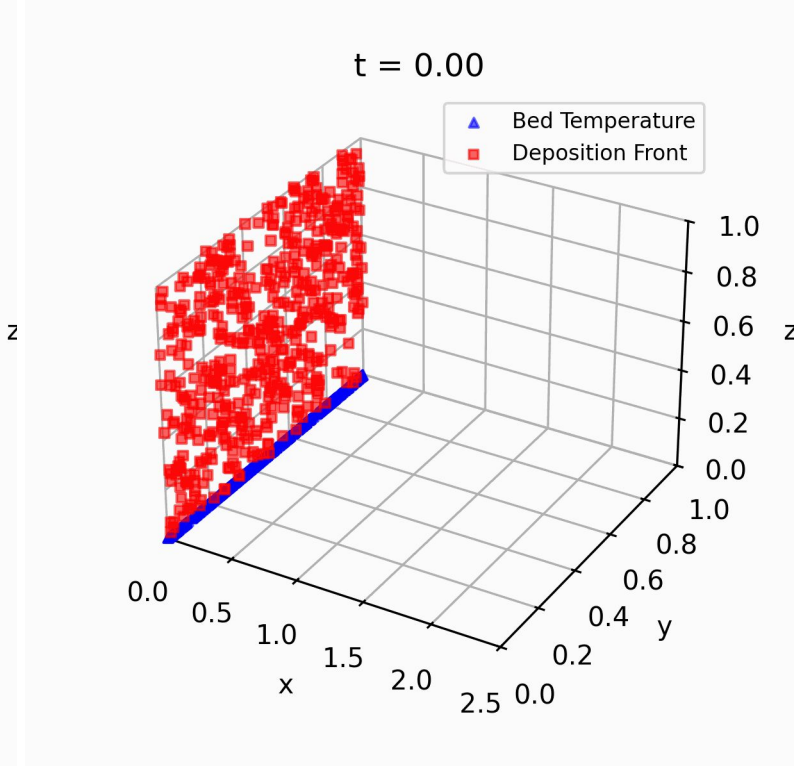
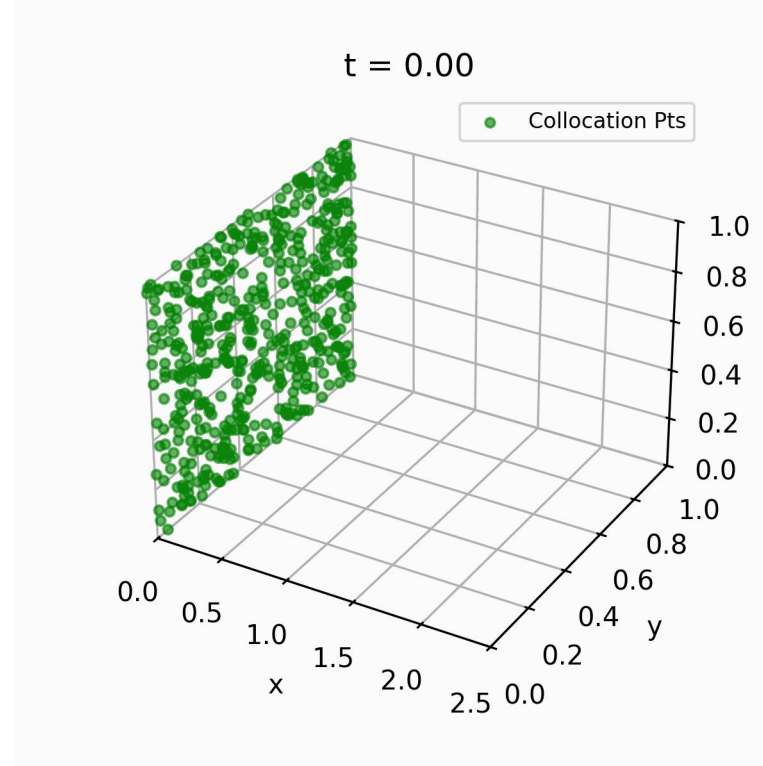
1. Constant **deposition surface**
2. Evolving **bed surface**
3. Constant and more evolving surfaces with *convection + radiation*

Case 1

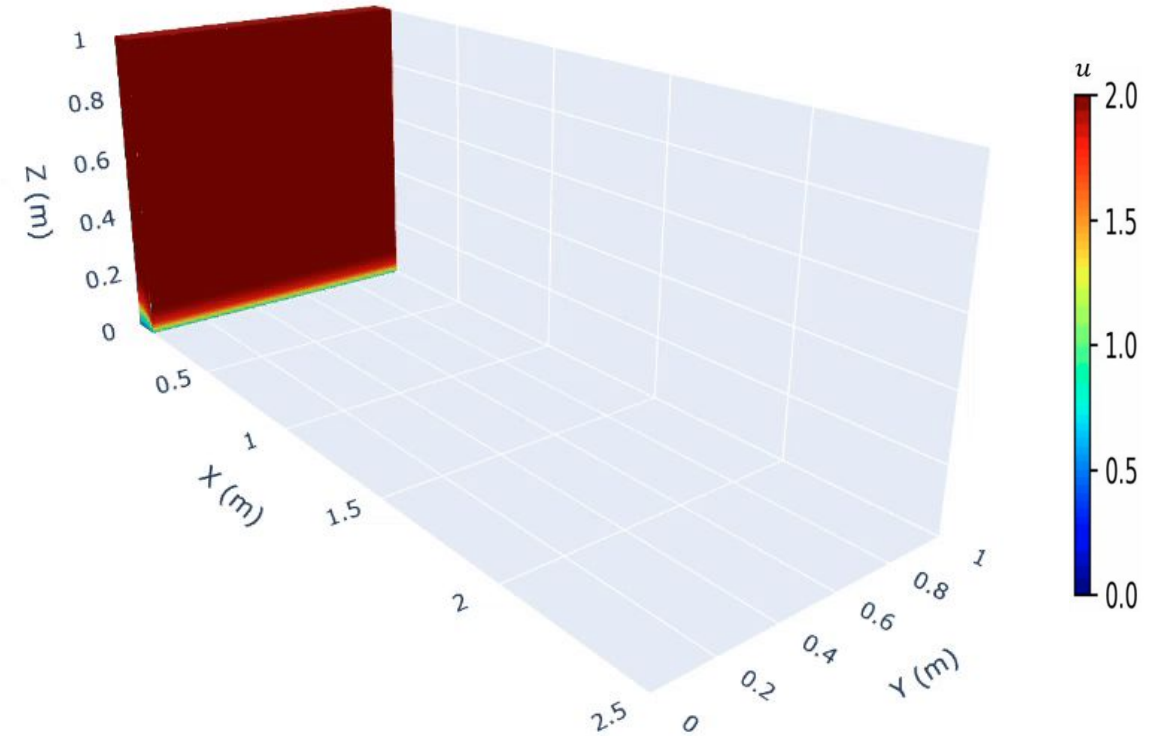
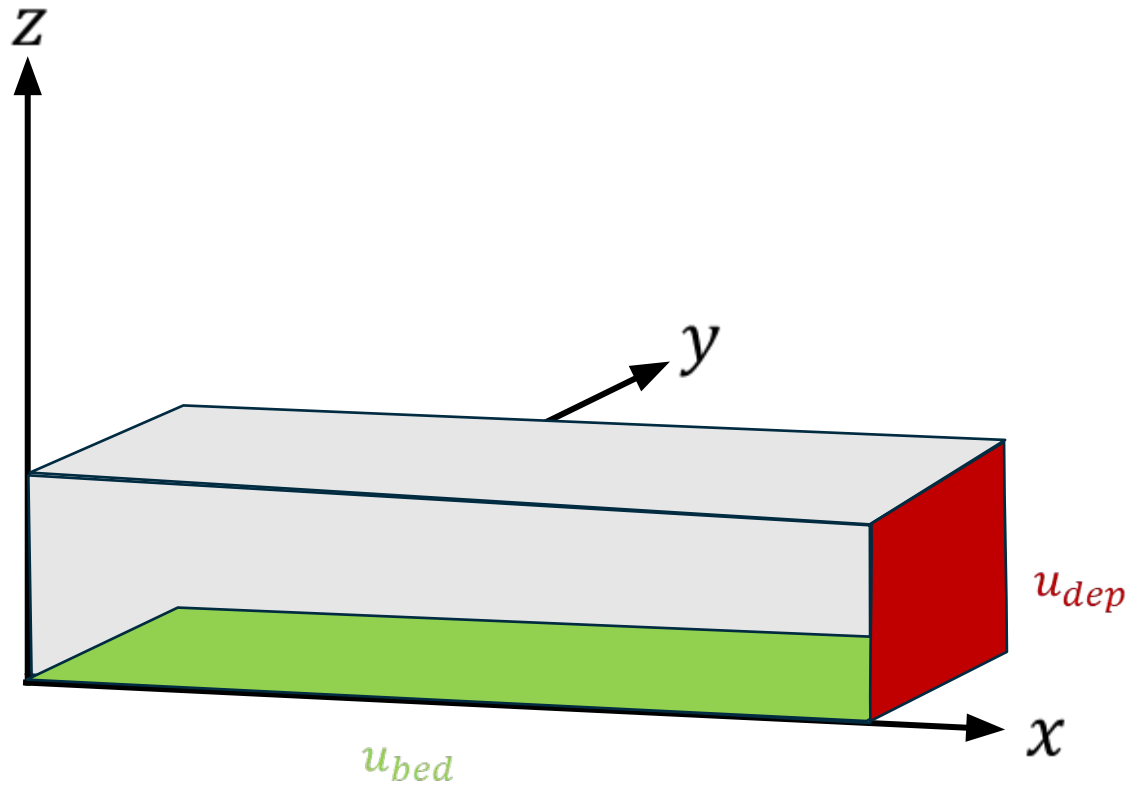


Conditions enforced:

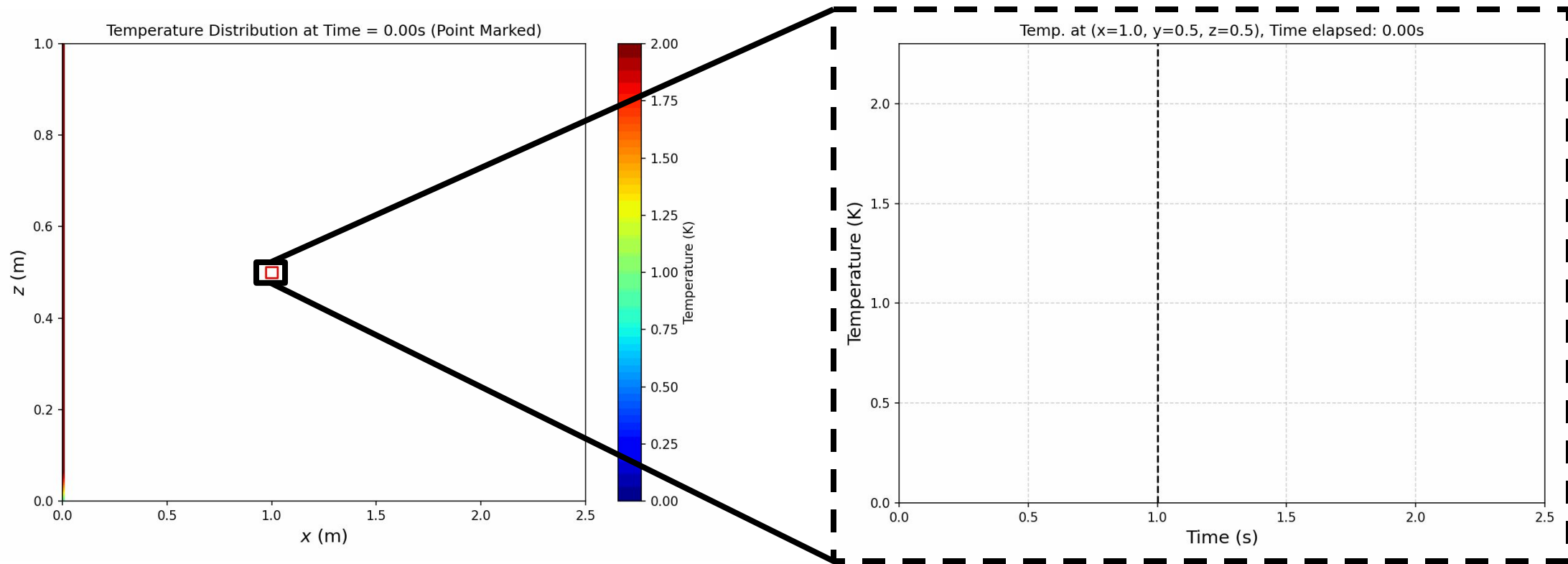
1. Constant **deposition surface**
2. Evolving **bed surface**



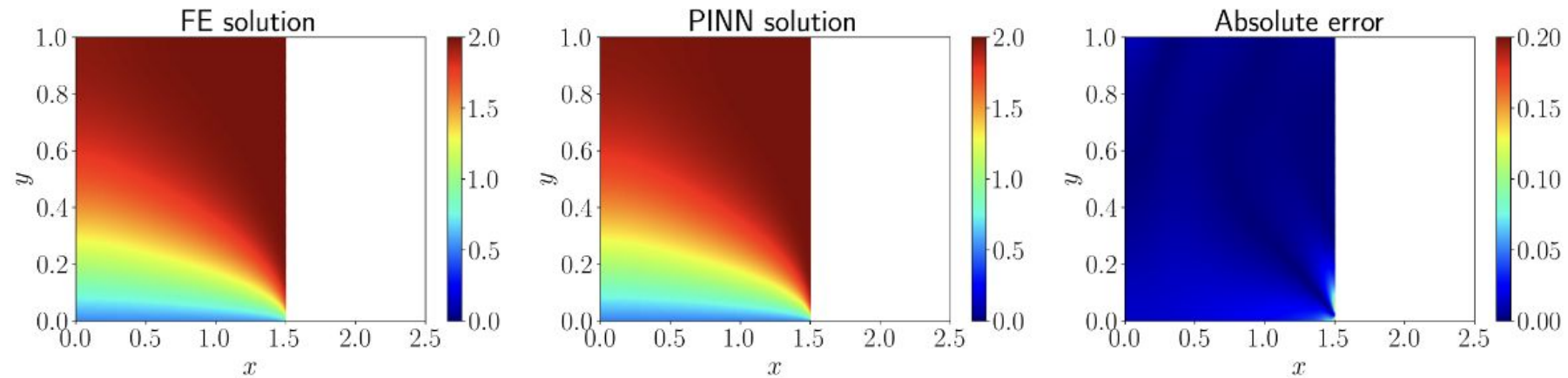
Visual Result: Case 1



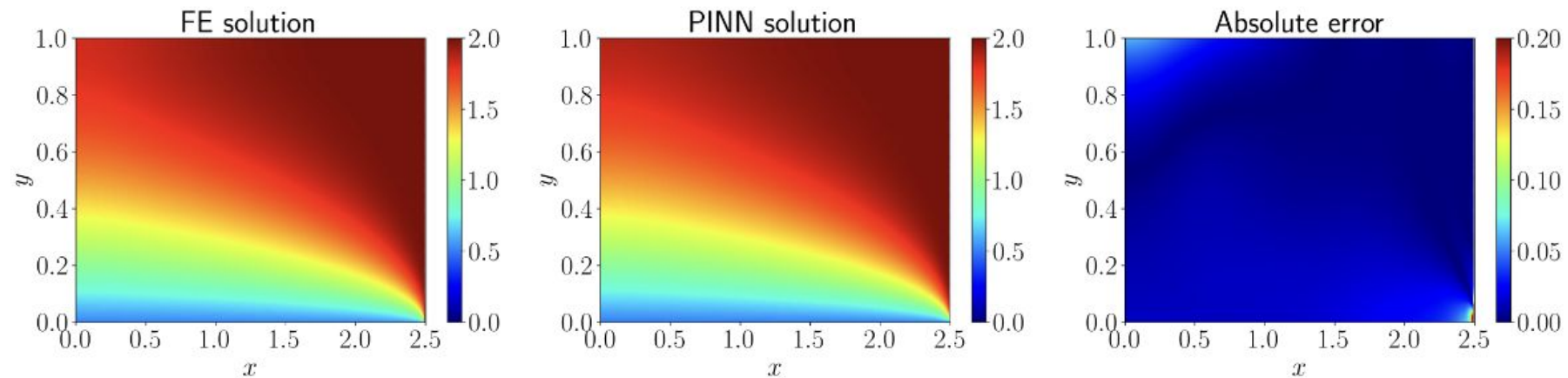
Visual Result: Case 1



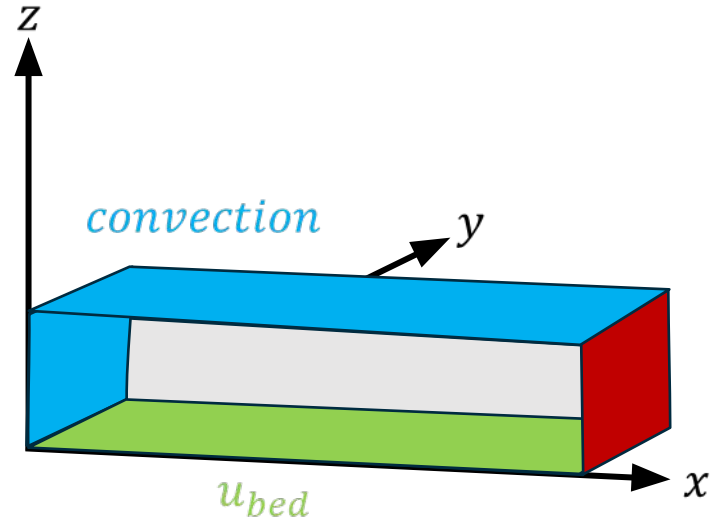
Comparison with FEM: Case 1



(c) At $t = 1.5$

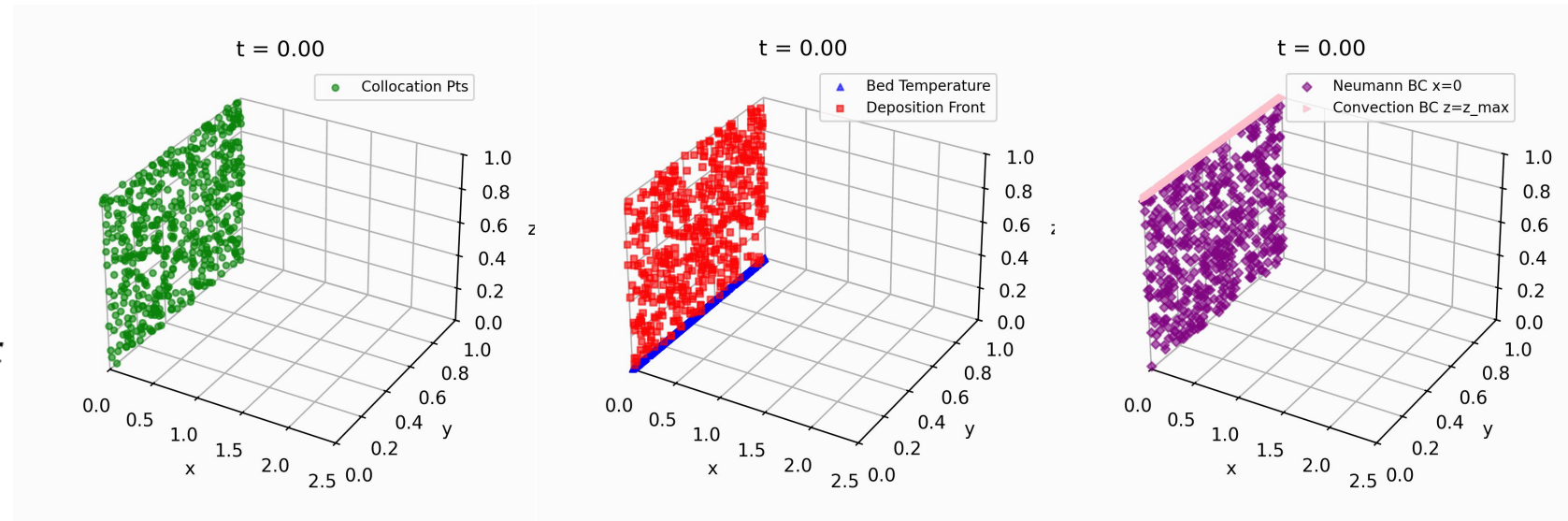


Case 2

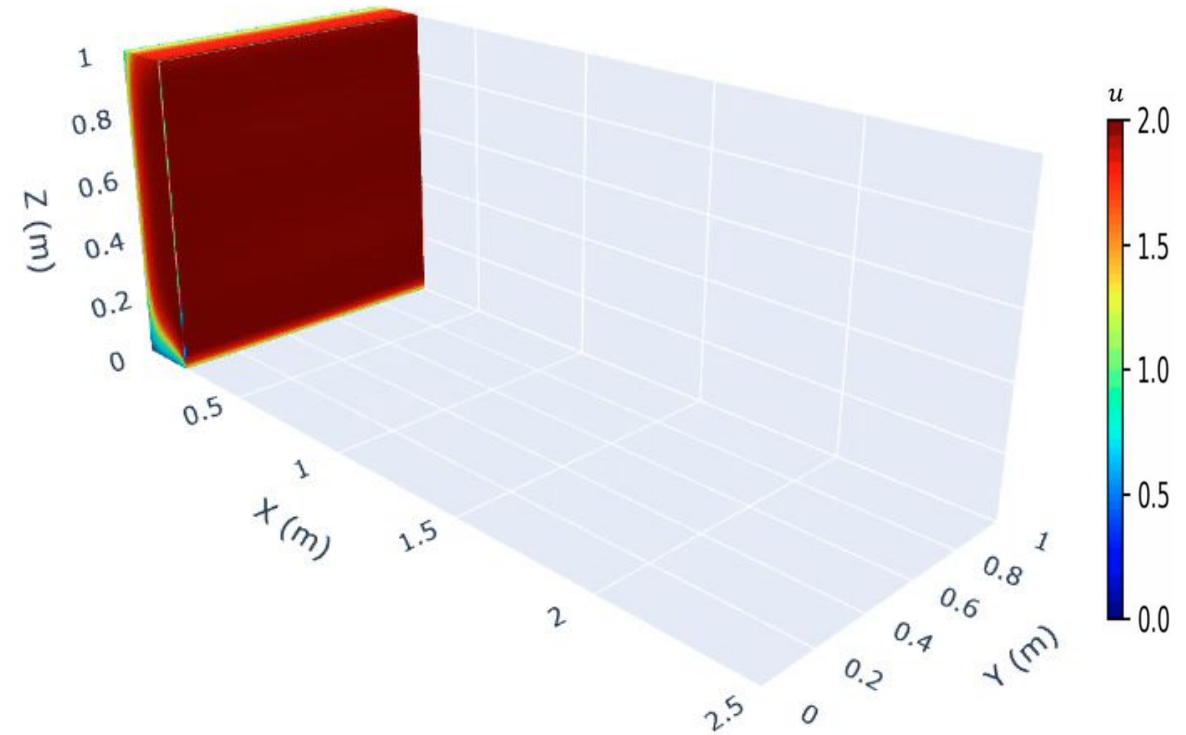
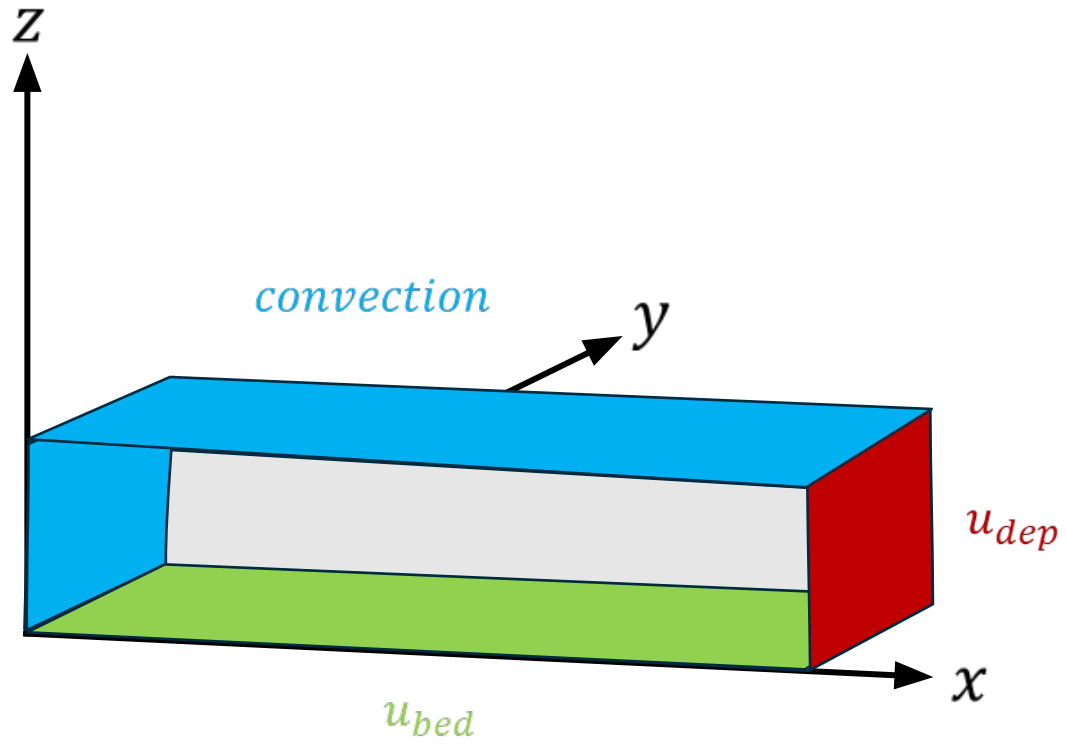


Conditions enforced:

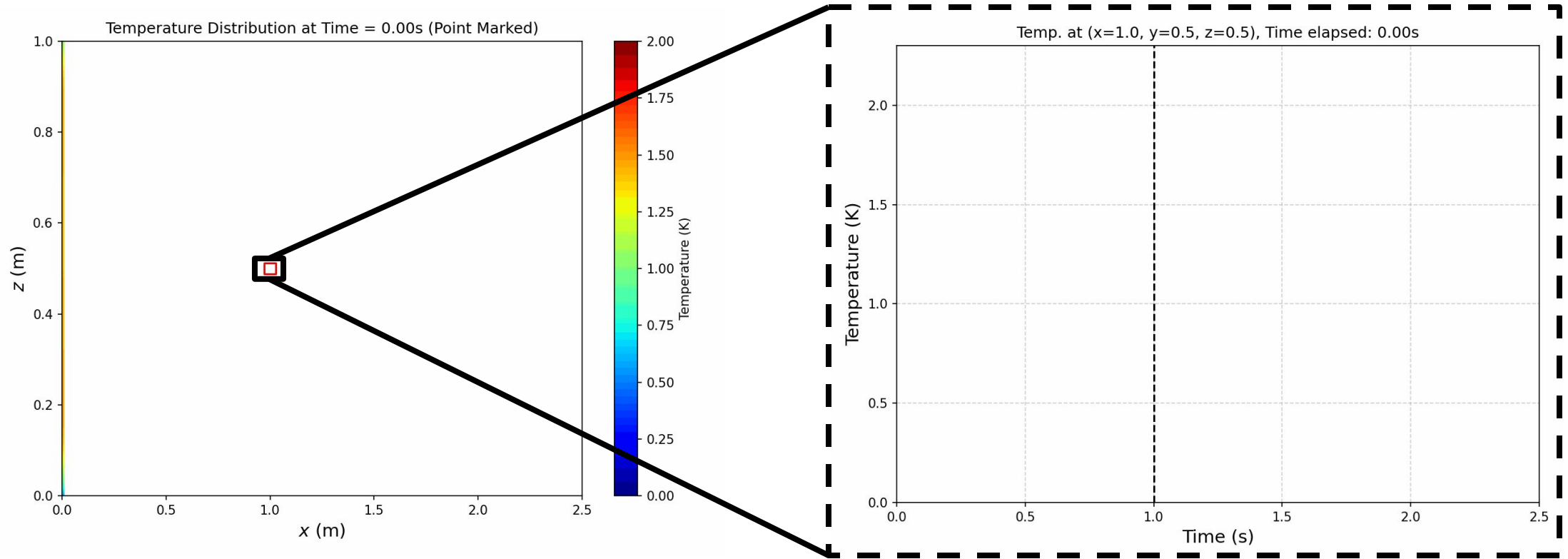
1. Constant **deposition surface**
2. Evolving **bed surface**
3. Constant and evolving surfaces with **convection**



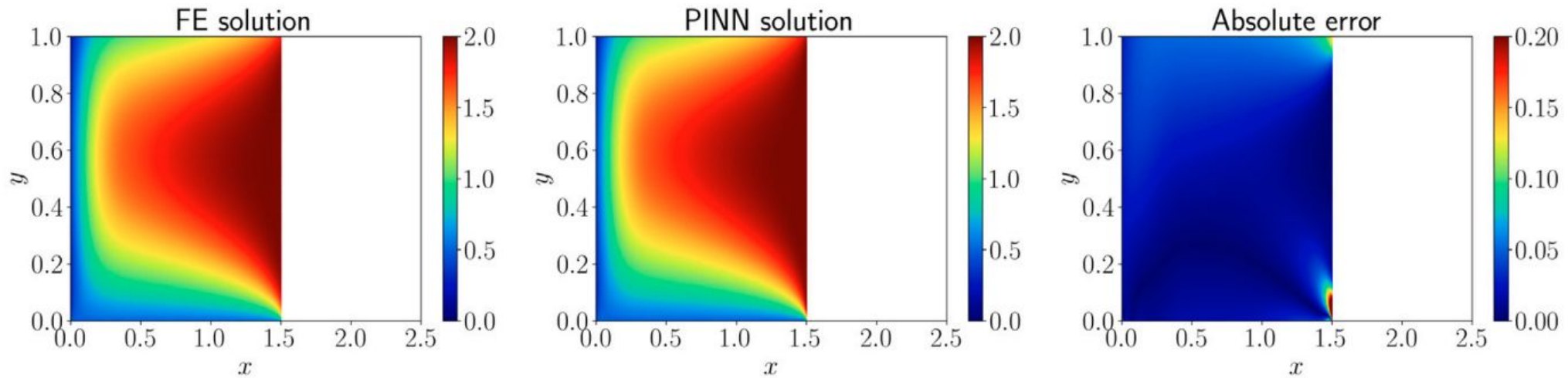
Visual Result: Case 2



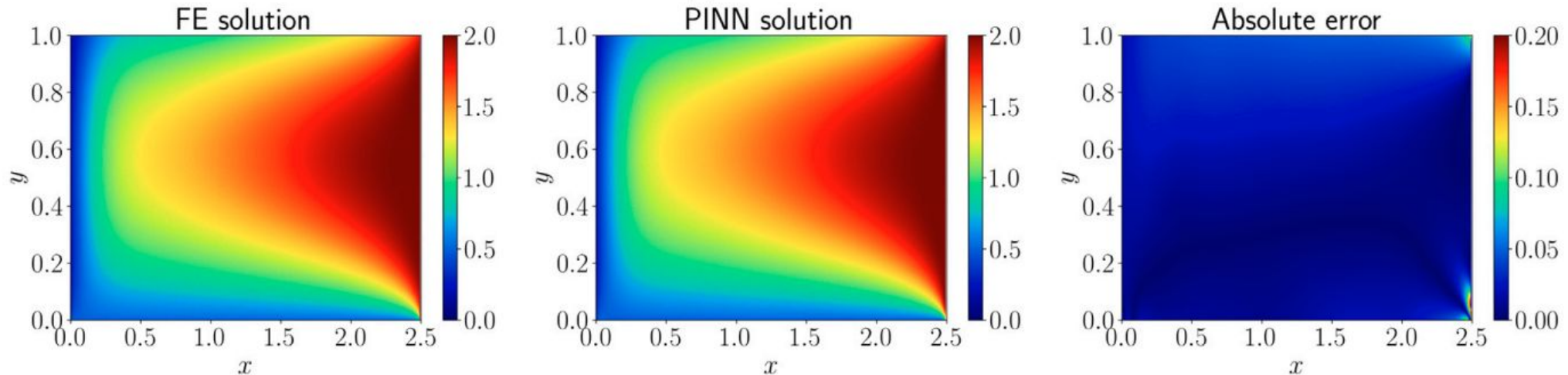
Visual Result: Case 2



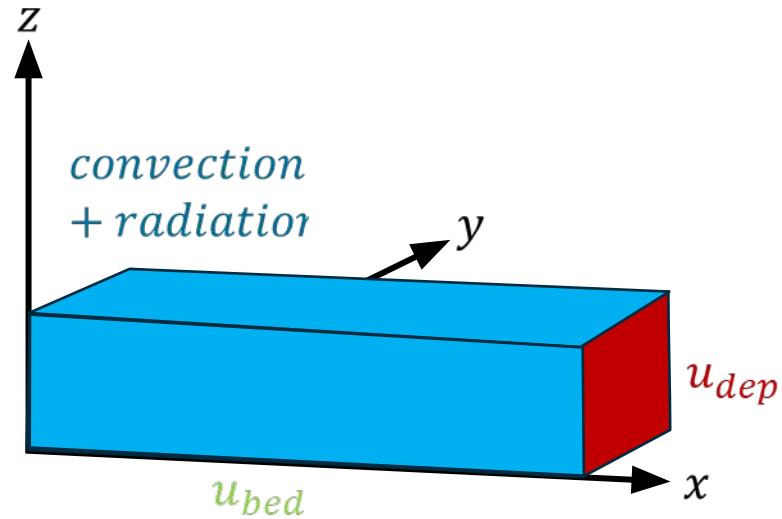
Comparison with FEM: Case 2



(b) At $t = 1.5$

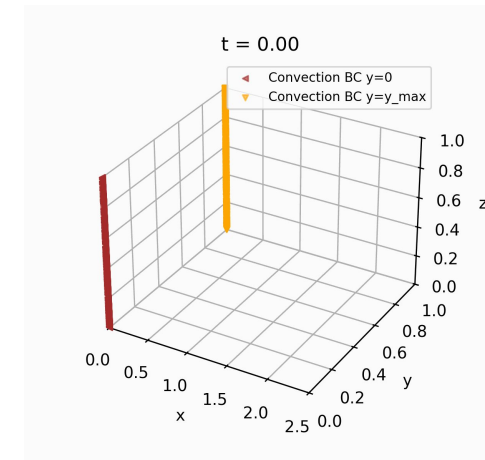
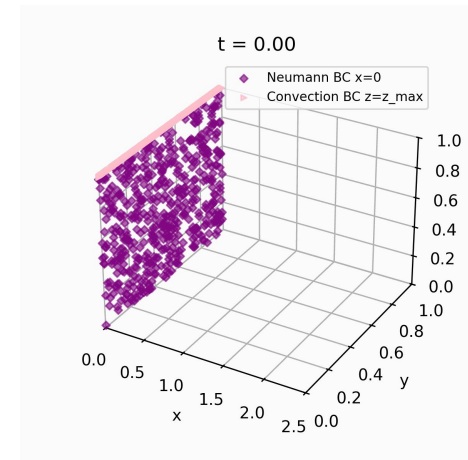
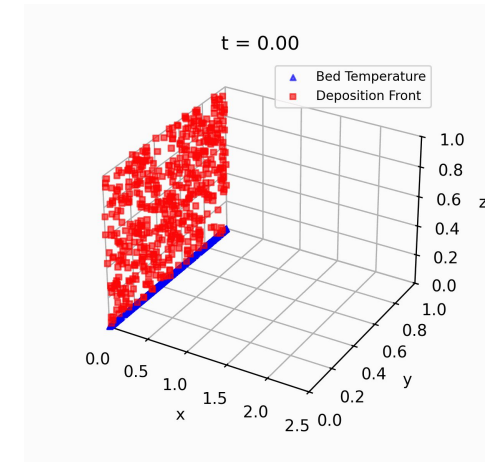
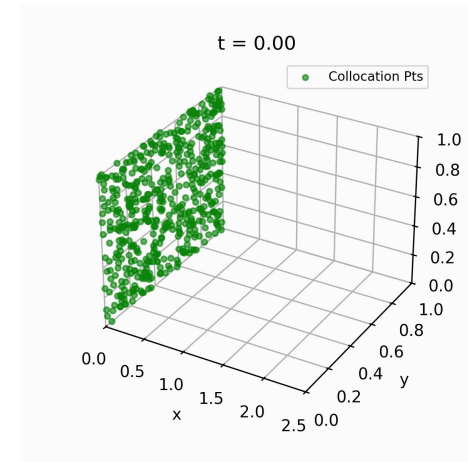


Case 3

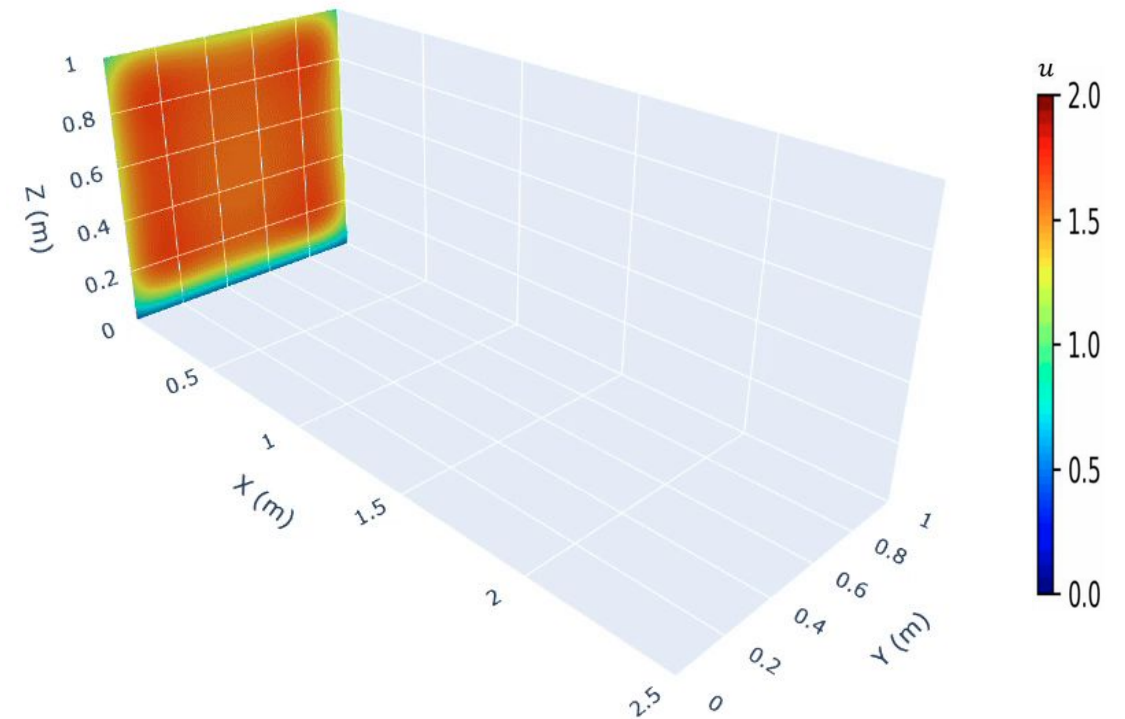
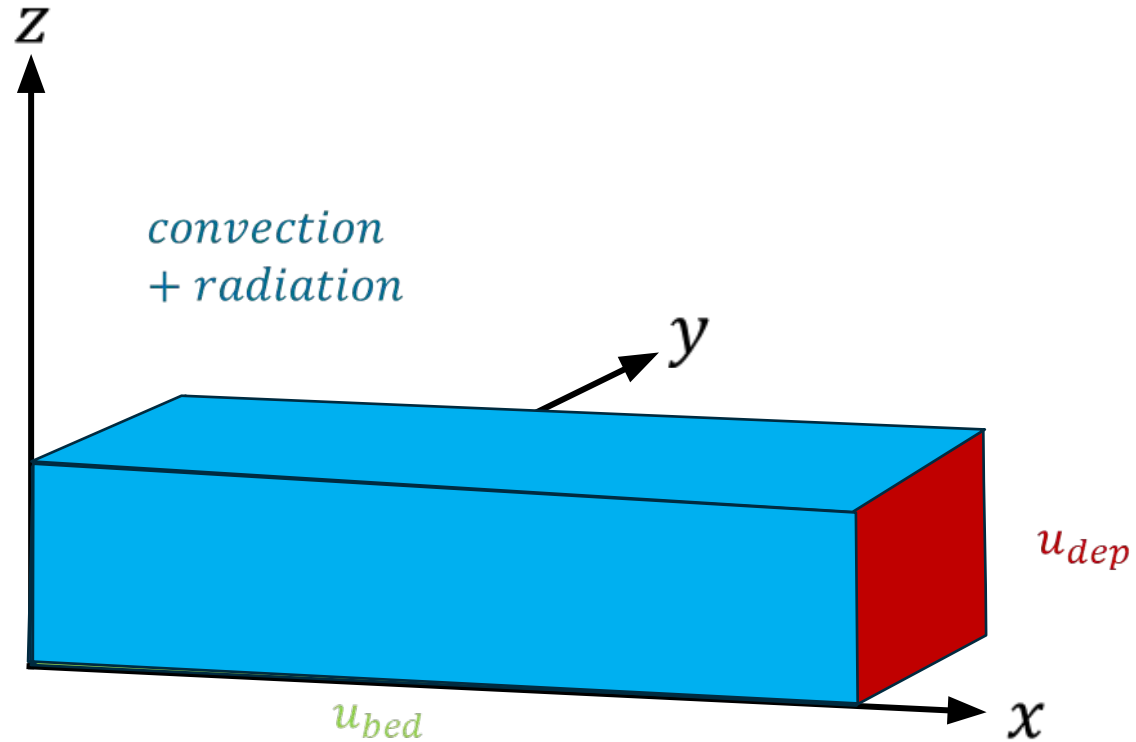


Conditions enforced:

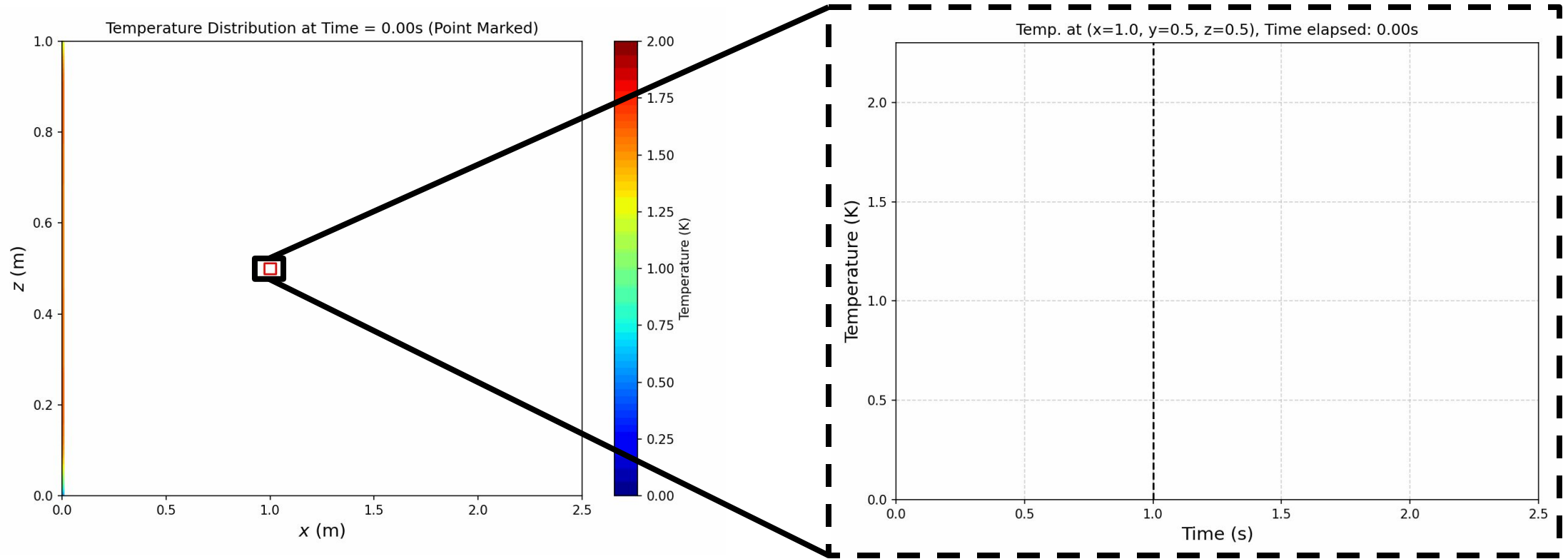
1. Constant **deposition surface**
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3. Constant and more evolving surfaces with **convection + radiation**



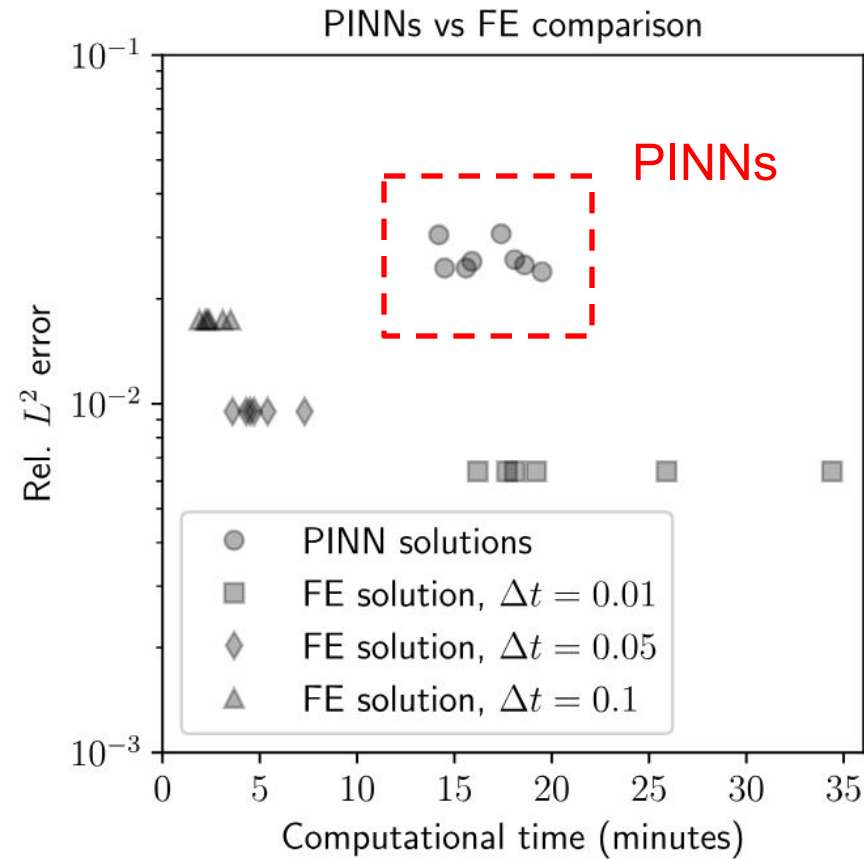
Visual Result: Case 3



Visual Result: Case 3



Computational Time



Parametric Problems

- Material properties or process conditions have inherent variability
 - e.g. Deposition temperature, Bed temperature, Convection coefficient, Thermal conductivity... etc.
- Aim is to see how the temperature field changes across a range of these parameters

Parametric PINNs

- A single PINNs can learn the solution across a range of these parameters
- The parameters are additional inputs to the NN

New loss function for parametric problems:

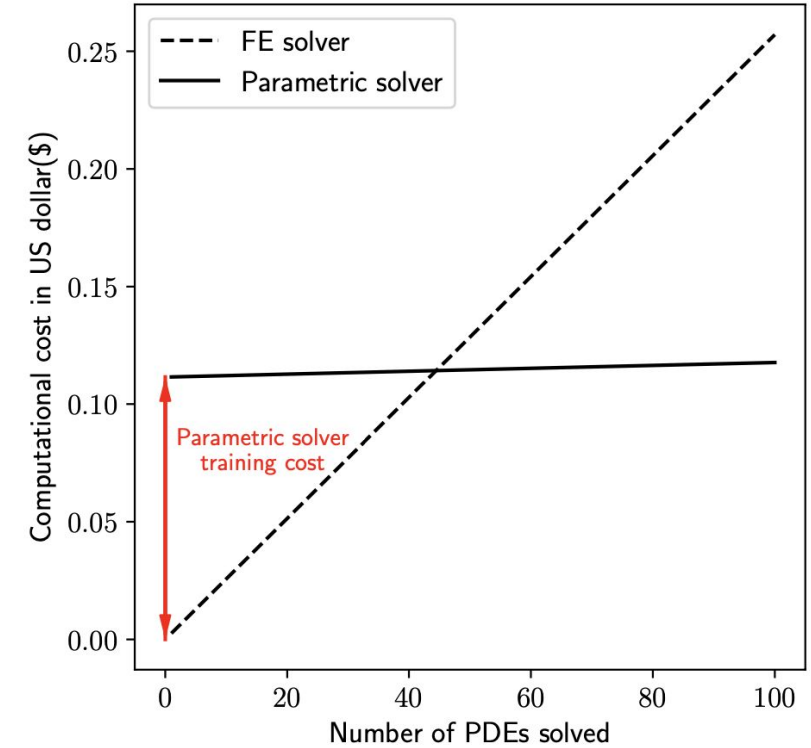
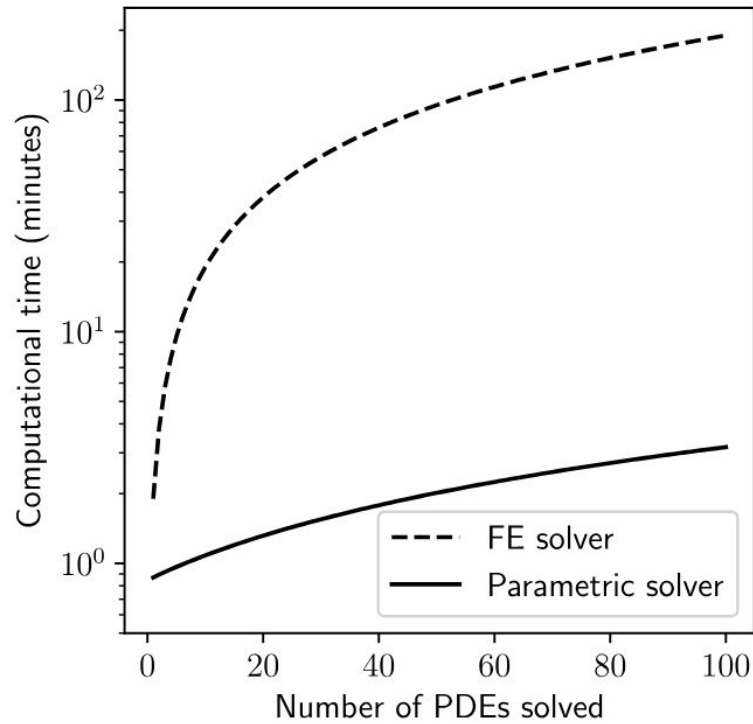
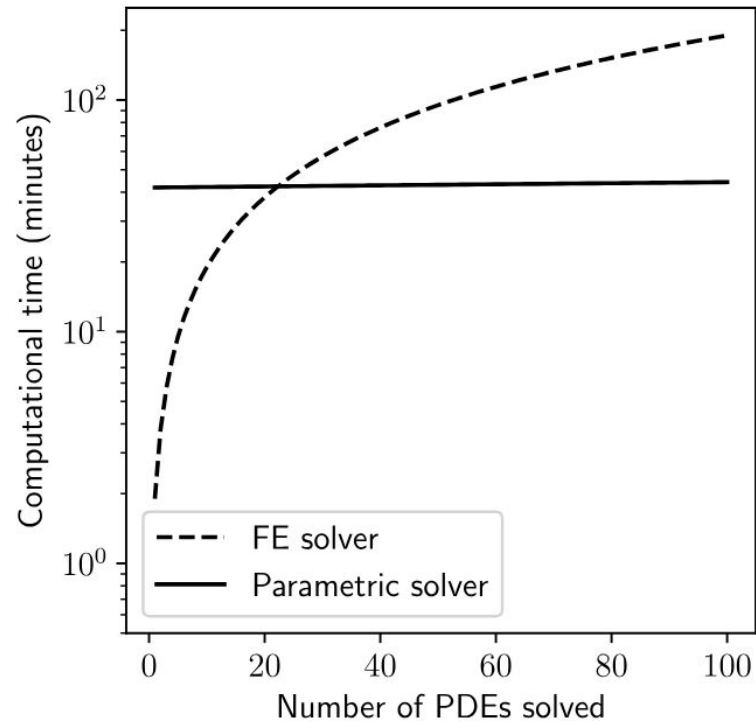
$$l_e = \int d\xi \int_0^T dt \, l(t, x(t), \xi_v; \theta)$$

Temperature field is parametrized as:

$$u_\theta(\tilde{t}, \tilde{\mathbf{x}}, \tilde{\xi}; \theta) = \sum_{i=1}^g \underbrace{\psi_i(\tilde{\xi}; \theta)}_{\text{branch}} \underbrace{\phi_i(\tilde{t}, \tilde{\mathbf{x}}; \theta)}_{\text{trunk}}$$

Once trained, predicting the solution for any new set of parameters is almost immediate!

Parametric Solver



Conclusion

- PINNs offer a **mesh-free** framework for **3D** heat transfer problem with **evolving geometries** and **complex boundary conditions**
- FEM is **faster** and **more accurate** for single forward problems
- PINNs have potential for **parametric** problems

Future Work

- Extension to arbitrary geometries
- Extension to multi-layer deposition

We aim to build surrogate models without having to run FEM

Thank you!

J. Kil et al. (2025) "Physics-informed neural networks to accelerate heat transfer predictions in additive manufacturing"

A. J. Thomas et al. (2025) "Causality enforcing parametric heat transfer solvers for evolving geometries in advanced manufacturing"

